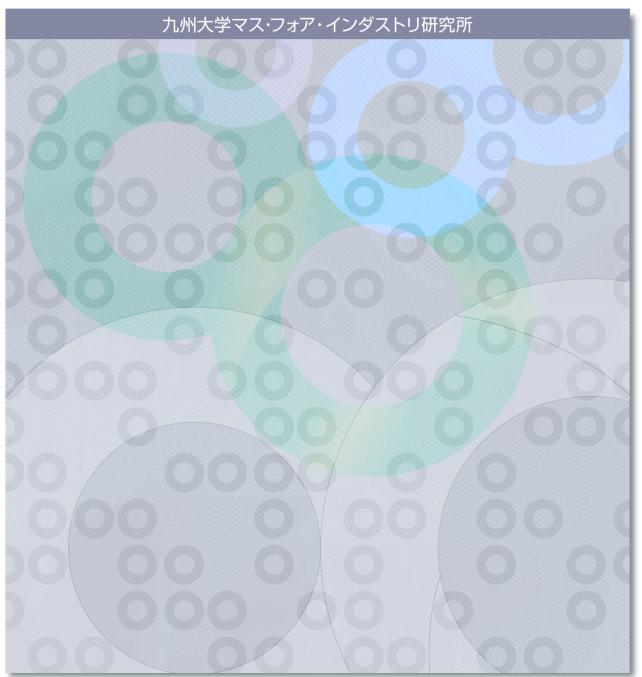


IMI Workshop of the Joint Usage Research Projects **Exploring Mathematical and Practical Principles of Secure Computation and Secret Sharing**

Editors: Hiroaki Anada, Yasuhiko Ikematsu, Koji Nuida, Satsuya Ohata, Yuntao Wang



IMI Workshop of the Joint Usage Research Projects Exploring Mathematical and Practical Principles of Secure Computation and Secret Sharing

Editors:

Hiroaki Anada, Yasuhiko Ikematsu, Koji Nuida, Satsuya Ohata, Yuntao Wang

About MI Lecture Note Series

The Math-for-Industry (MI) Lecture Note Series is the successor to the COE Lecture Notes, which were published for the 21st COE Program "Development of Dynamic Mathematics with High Functionality," sponsored by Japan's Ministry of Education, Culture, Sports, Science and Technology (MEXT) from 2003 to 2007. The MI Lecture Note Series has published the notes of lectures organized under the following two programs: "Training Program for Ph.D. and New Master's Degree in Mathematics as Required by Industry," adopted as a Support Program for Improving Graduate School Education by MEXT from 2007 to 2009; and "Education-and-Research Hub for Mathematics-for-Industry," adopted as a Global COE Program by MEXT from 2008 to 2012.

In accordance with the establishment of the Institute of Mathematics for Industry (IMI) in April 2011 and the authorization of IMI's Joint Research Center for Advanced and Fundamental Mathematics-for-Industry as a MEXT Joint Usage / Research Center in April 2013, hereafter the MI Lecture Notes Series will publish lecture notes and proceedings by worldwide researchers of MI to contribute to the development of MI.

October 2018 Osamu Saeki Director Institute of Mathematics for Industry

IMI Workshop of the Joint Usage Research Projects

Exploring Mathematical and Practical Principles of Secure Computation and Secret Sharing

MI Lecture Note Vol.85, Institute of Mathematics for Industry, Kyushu University ISSN 2188-1200 Date of issue: February 9, 2022 Editors: Hiroaki Anada, Yasuhiko Ikematsu, Koji Nuida, Satsuya Ohata, Yuntao Wang Publisher: Institute of Mathematics for Industry, Kyushu University Graduate School of Mathematics, Kyushu University Motooka 744, Nishi-ku, Fukuoka, 819-0395, JAPAN Tel +81-(0)92-802-4402, Fax +81-(0)92-802-4405 URL https://www.imi.kyushu-u.ac.jp/

Preface

As operation of the ultra-high speed and ultra-low delay fifth generation communication service begins in countries of the world, the expectation to a cryptographic technology increases in our society. For example, there is demand of treating data with a guarantee that no leakage of private information arise in the analysis handling customer data across their organizations. To meet the nee, secure computation in cryptology is being developed by companies, aiming practical application of commercial level. As another example, secret sharing that can, in theory, attain confidentiality and reliability of cloud storage is being developed to obtain more availability and efficiency. However, these developments are at an intermediate point of the spiral intertwined with research activity.

For the techniques of secure computation and secret sharing to be taken in and to be used actually, mathematical investigation, rigorous security proofs and recapturing usage performance are indispensable. Especially, the following directions are important from the point of view of mathematics: (1) classifying mathematical approaches such as abstract algebra, information theory, coding theory, combinatorics and game theory; (2) mitigating assumptions of security, that is, semi-honest adversaries versus active adversaries, computational security versus information-theoretic security, etc.; (3) improving efficiency, that is, decreasing computational amount, communication cost, the number of rounds and complexity of randomness.

The purpose of this workshop was to gather researchers in industry and academia in order to share their experience on mathematical approaches and practical implementations of secure computation and secret sharing for securing distributed data processing and data storage. Then the participants discussed the actual problems which the industry was facing when implementing the cryptographic technologies. Also, they discussed the appropriate solutions. The workshop consisted of the invited lectures and tutorials on recent results of secure computation and secret sharing. We hope that this lecture note would help readers obtain some intuition in the technologies.

Hiroaki Anada, Representative of the Organizers

Acknowledgements

This work was supported by 2021 IMI Joint Use Research Program Workshop (I) "Exploring Mathematical and Practical Principles of Secure Computation and Secret Sharing".



IMI Joint Research Project in 2021



Exploring Mathematical4and Practical Principles7of Secure Computation7and Secret Sharing1

November 8(Mon)-10(Wed), 2021

Keynote speaker:

Johannes BUCHMANN, Technische Universität Darmstadt "Cryptographic long-term security"

Invited speakers:

Reo ERIGUCHI, The University of Tokyo Keitaro HIWATASHI, The University of Tokyo Kosuke KANEKO, Robert T.Huang Entrepreneurship Center of Kyushu University Yi LU, Tokyo Institute of Technology Ibuki MISHINA, NTT Social Informatics Laboratories Kirill MOROZOV, University of North Texas Hikaru TSUCHIDA, NEC Corporation

Venue: Online

■Organizing Committee ► Hiroaki ANADA, University of Nagasaki



Hiroaki ANADA, University of Nagasaki
 Yasuhiko IKEMATSU, Institute of Mathematics for Industry, Kyushu University
 Koji NUIDA, Institute of Mathematics for Industry, Kyushu University
 Satsuya OHATA
 Yuntao WANG, Japan Advanced Institute of Science and Technology

■Sponsored by ▶ Institute of Mathematics for Industry, Kyushu University

Registration fee
Free

https://www.imi.kyushu-u.ac.jp/kyodo-riyo/research_meetings/view/30

Contact : imikyoten@jimu.kyushu-u.ac.jp (For general inquiries) Institute of Mathematics for Industry, Kyushu University

九州大学 IMI 共同利用·研究集会(I)

秘密計算・秘密分散の数理と実用の探求

Exploring Mathematical and Practical Principles

of Secure Computation and Secret Sharing

Η 時: 2021年11月08日(月)16:00~18:25 2021年11月09日 (火) 09:00 ~ 11:25 2021年11月10日(水)16:00~18:15 場 Zoomによるオンライン開催 所: 組織委員 : Hiroaki Anada (University of Nagasaki) (研究代表者) Yasuhiko Ikematsu (IMI, Kyushu University) Koji Nuida (IMI, Kyushu University) Satsuya Ohata

• Yuntao Wang (Japan Advanced Institute of Science and Technology)

プログラム

<u>11月08日(月)</u>

16:00-16:05 オープニング

16:05-16:55

講演者:Johannes Buchmann(Technische Universität Darmstadt) 講演タイトル:"Cryptographic Long-Term Security"

17:05-17:40

講演者:Yi Lu (Tokyo Institute of Technology / National Institute of Advanced Industrial Science and Technology) 講演タイトル: "Efficient Two-party Exponentiation from Quotient Transfer"

17:50-18:25 講演者:Hikaru Tsuchida (NEC Corporation) 講演タイトル: "General-purpose Compiler for Secure Three-party Computation and Its Application to Prediction by Machine Learning Model"

<u>11月09日(火)</u>

09:00-09:05 第2日オープニング

09:05-09:55 講演者:Kirill Morozov(University of North Texas) 講演タイトル:"Evolving Secret Sharing From Evolving Perfect Hash Families" 10:05-10:40 講演者:Ibuki Mishina (NTT Social Informatics Laboratories) 講演タイトル: "Secure-Computation AI : a Python Library for Machine Learning in Secure Computation"

10:50-11:25 講演者:Kosuke Kaneko(Robert T.Huang Entrepreneurship Center of Kyushu University)

講演タイトル: "Possibility of Secret Sharing using EtherCAT"

11月10日(水)

16:00-16:05 第3日オープニング

16:05-16:40

講演者:Yasuhiko Ikematsu (Institute of Mathematics for Industry) 講演タイトル:"An Indeterminate Equation Scheme having Homomorphic Property"

16:50-17:25

講演者:Reo Eriguchi (The University of Tokyo) 講演タイトル: "Homomorphic Secret Sharing for Multipartite and General Adversary Structures Supporting Parallel Evaluation of Low-Degree Polynomials"

17:35-18:10 講演者:Hiroaki Anada (University of Nagasaki) 講演タイトル:"A Comparison of How to Garble Arithmetic and Boolean Circuits"

18:10-18:15 クロージング

最新情報及び参加情報は下記 URL(QR コード)のウェブサイトにて御確認下さい. https://www.imi.kyushu-u.ac.jp/kyodo-riyo/research_meetings/view/30



Contents

Cryptographic Long-term Security 1 Johannes Buchmann (Technische Universität Darmstadt)
Efficient Two-party Exponentiation from Quotient Transfer
General-purpose Compiler for Secure Three-party Computation and Its Application to Prediction by Machine Learning Model Hikaru Tsuchida (NEC Corporation)
Evolving Secret Sharing From Evolving Perfect Hash Families
Secure-Computation AI: a Python Library for Machine Learning in Secure Computation 63 Ibuki Mishina (Joint work with Dai Ikarashi, Koki Hamada and Ryo Kikuchi) (NTT Corporation)
Possibility of Secret Sharing using EtherCAT 73 Kosuke Kaneko (Robert T. Huang Entrepreneurship Center of Kyushu University)
An indeterminate equation scheme having homomorphic property
Homomorphic Secret Sharing for Multipartite and General Adversary Structures Supporting Parallel Evaluation of Low-Degree Polynomials
A Comparison of How to Garble Arithmetic and Boolean Circuits - Case of Functional Encryption - 105 Hiroaki Anada (Joint work with Kotaro Chinen) (University of Nagasaki)

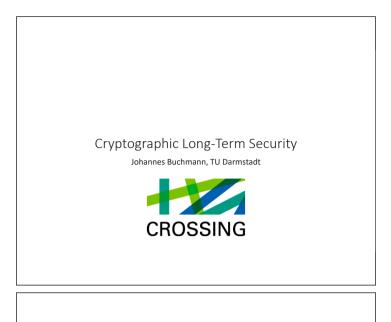
November 8–10, 2021, Kyushu University

Cryptographic Long-term Security

Johannes Buchmann

Technische Universität Darmstadt johannes.buchmann@tu-darmstadt.de

Digitization is omnipresent and all important areas of our private, political, social, and economic lives depend on it. As a result, digitization must meet ever greater security requirements. In particular, security must be guaranteed for a very long period of time. One important technology that enables cybersecurity is cryptography. In the talk, I talk about how cryptography can enable long-term protection and the important role Secret Sharing plays in this.



The challenge

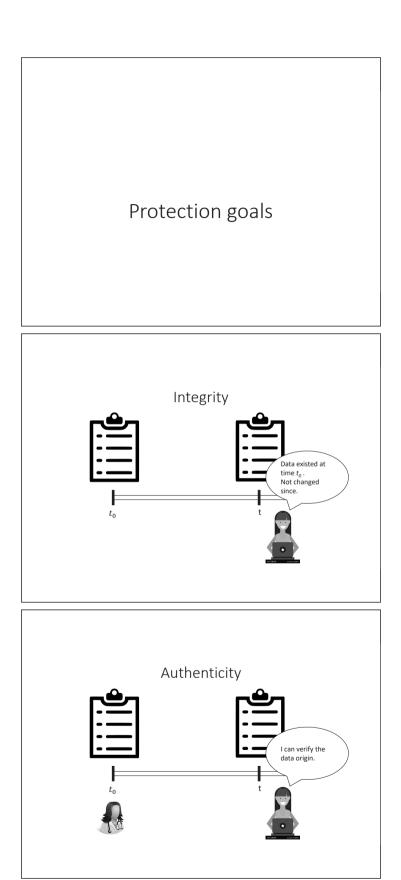
Japan Agency for Medical Research and Development

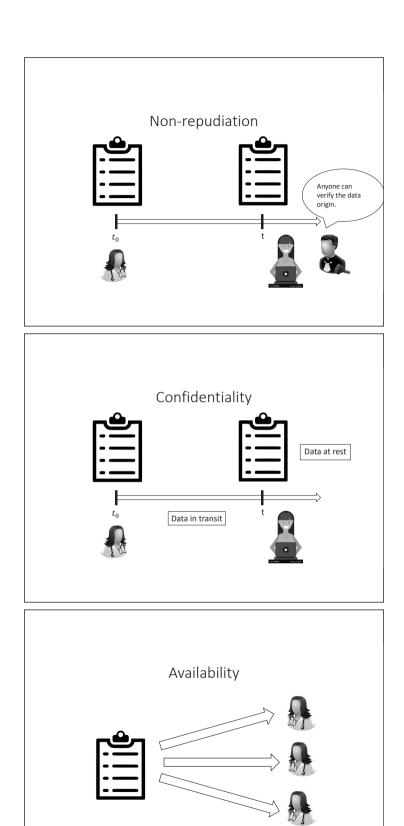
Project for Genome and Health Related Data Requires long-term protection!

Overview

AMED

Toward realization of personalized medicine, this project procedue the development and ublication of genome liels infeathuritures and supports R&D that contributes to the proceeding, diagraming and treatment of disease based on the relationship between genetic metations and polymorphism and the development of diseases, from a life-stage perspective.





Protection by cryptography

Protection goal	Cryptographic method
Confidentiality	Encryption + key exchange
Integrity	Hash, MAC, digital signature
Authenticity	MAC, digital signature
Non-repudiation	Digital signature
Availability	

Today's cryptography is complexity-based

Cryptographic method	Algorithms	Hard problem
Key Exchange	RSA/Diffie-Hellman	Factoring/Discrete Logarithm
+ Encryption	AES	AES
Hash, MAC	SHA-3, HMAC	SHA-3
Digital signature	RSA, ECDSA	Factoring, EC-DL

Today's complexity-based cryptography is not sustainable

Algorithm	Standardized	Broken	Ву	Lifetime
DES	1977	1997	Brute force	20 years
Diffie-Hellman	1999	2030?	Quantum computer	31 years?
MD5	1992	1996/2004	Analysis of algorithm	4 years
RSA	1991	2030?	Quantum computer	39 years?
RSA-512		2000	Number Field Sieve	9 years
ECDSA	2005	2030?	Quantum computer	25 years?

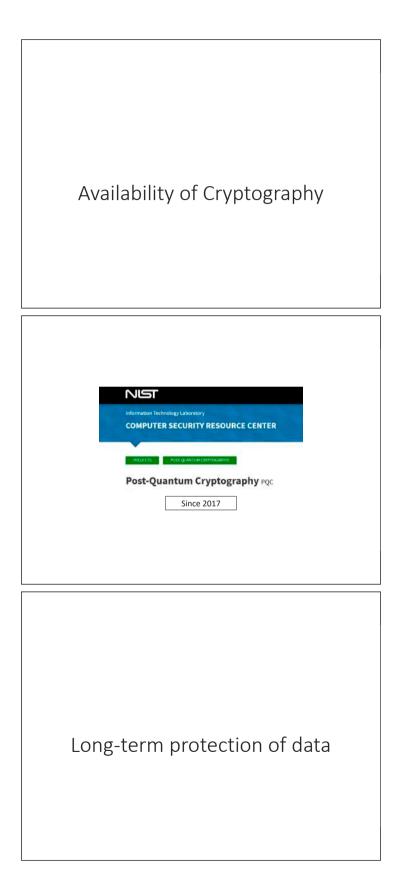
Aspects of cryptographic long-term security

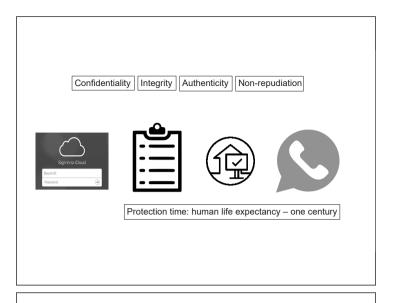


new attacks

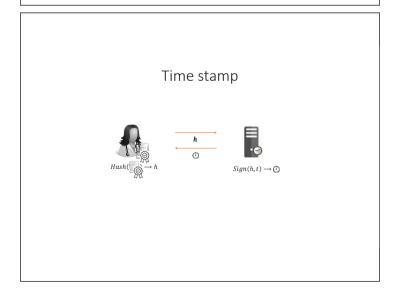


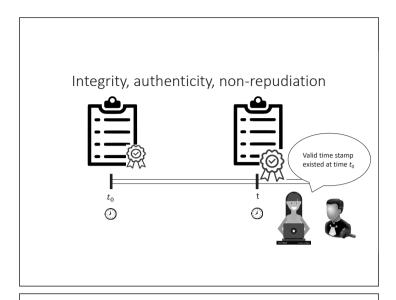
Long-term protection of data





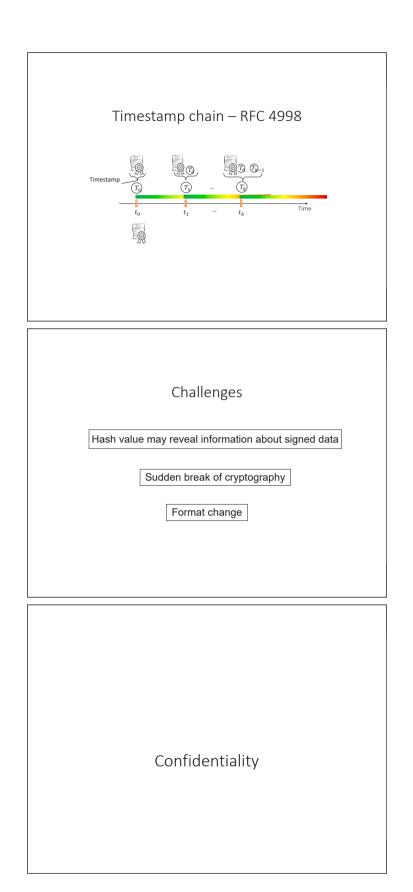
Integrity, authenticity, non-repudiation





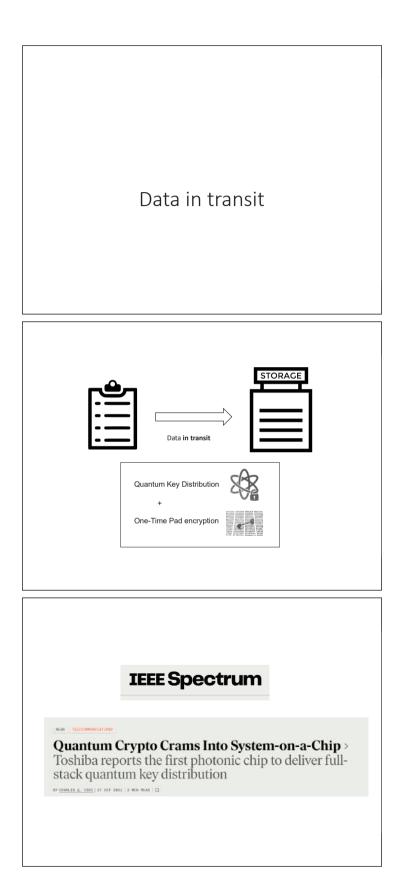
Time stamps use signatures which are not long-term

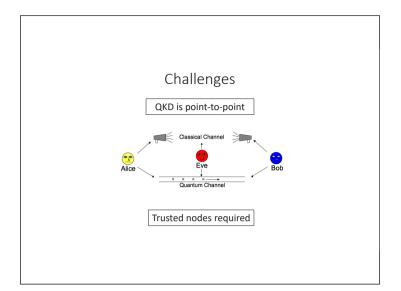
Time stamp security can be prolonged!

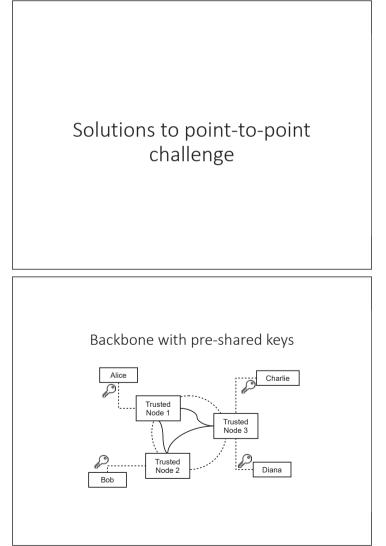


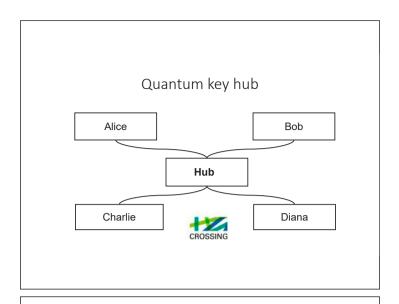
Encryption	
Data in transit	Data at rest
Long-term secure?	

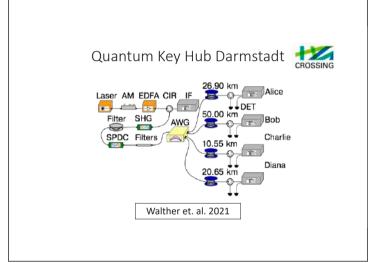
The Wo	GYBERCRIME MAGAZINE orld Will Store 200 Zettabytes Of Data By 2025
	200 Zettabytes = 2*10 ²³ Bytes ~ 200 TB/Person in the world
	Cyphertexts may be stored now and can be decrypted later
	Encryption security cannot be prolonged
Infor	mation theoretic confidentiality protection is required



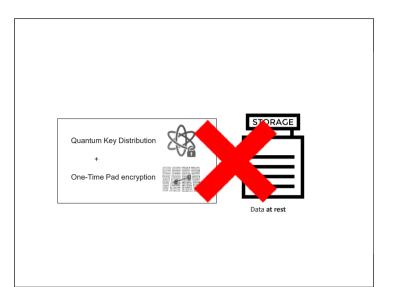




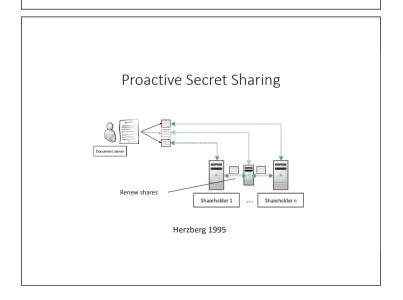


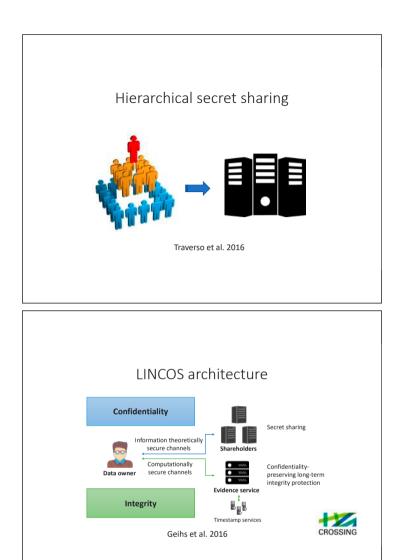


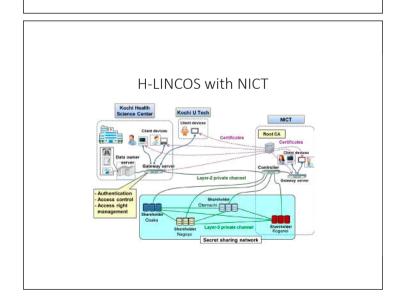


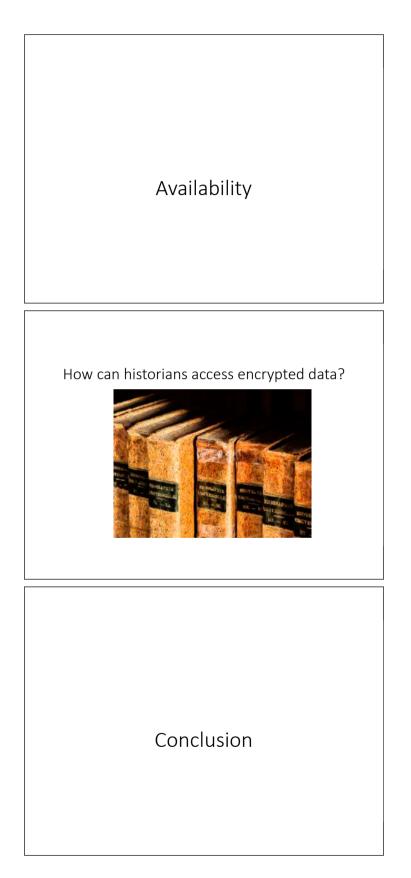


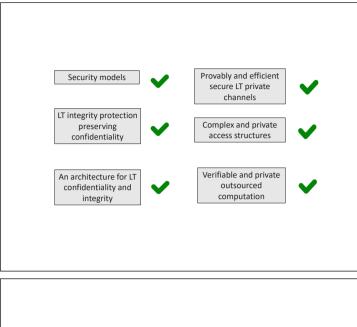
Solution: secret sharing

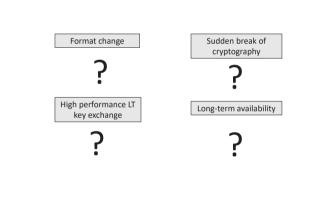












Thank you very much for your attention!



November 8-10, 2021, Kyushu University

Efficient Two-party Exponentiation from Quotient Transfer

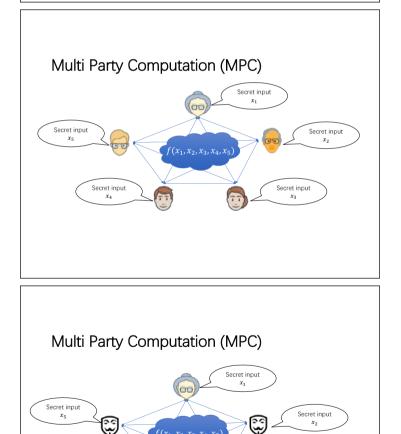
Yi Lu (Joint work with Keisuke Hara, Kazuma Ohara, Jacob Schuldt, and Keisuke Tanaka)

Tokyo Institute of Technology / National Institute of Advanced Industrial Science and Technology lu.y.ai@m.titech.ac.jp

Secure multi-party computation (MPC) allows participating parties to jointly compute a function over their inputs while keeping them private. In particular, MPC based on additive secret sharing has been widely studied as a tool to obtain efficient protocols secure against a dishonest majority, including the important two-party case. In this paper, we propose a two-party protocol for an exponentiation functionality based on an additive secret sharing scheme. Our proposed protocol is based on a new simple but efficient approach involving quotient transfer that allows the parties to perform the most expensive part of the computation locally. Our protocol requires 6 rounds and 4 invocations of multiplication. This is the first two-party protocol for an exponentiation functionality with constant-round efficiency based on an additive secret sharing scheme. As an intermediate primitive for our efficient two-party exponentiation protocol, we propose an efficient modulus conversion protocol, which may be of independent interest.

Efficient Two-party Exponentiation from Quotient Transfer

LU YI (Tokyo Tech/AIST) Hara Keisuke (Tokyo Tech/AIST) Ohara Kazuma (AIST) Jacob Schuldt (AIST) Tanaka Keisuke (Tokyo Tech)



 $f(x_1, x_2, x_3, x_4, x_5)$

Secret input

 x_3

Secret input

*x*₄

Basic Properties for MPC

- Correctness : the function is computed correctly
- •Security : Only the output is revealed

Modeling Adversaries

- Adversarial Behavior
 - Semi-honest : follows the protocol specification
 - Malicious : follows any arbitrary strategy
- Adversarial power
 - Polynomial-time : computational security
 - Computationally unbounded :
 - information-theoretic security

Modeling Adversaries

- Adversarial Number
 - Honest-Majority: The number of honest party is over half of all participants
 - Dishonest-Majority: The number of adversary is over half of all participants

Semi-honest and Computationally unbounded

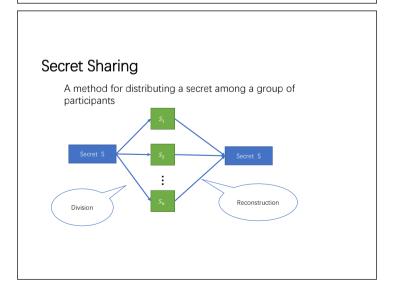
The performance of MPC

- Rounds: The number of communications, which can be done simultaneously will be counted as one round
- Communication Complexity: The number of bits which are transferred in communication The number of invocations of Multiplication.
- Computation Complexity: The number of computations which is done in protocol

Multi Party Computation (MPC)

Method	Communication Complexity	Rounds	Computation Complexity
Secret Sharing	small	big	small
FHE	big	small	big
Garbled Circuit(GC)	big	small	normal-big

Table 2. Three Method to Implement MPC



(k,n) threshold Secret Sharing Scheme

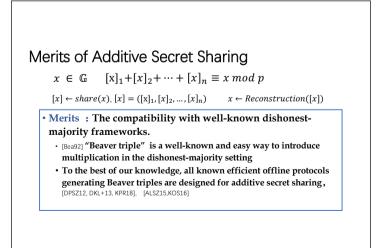
- Divide secret data (D) into pieces (n)
- Knowledge of some pieces (k) enables to derive secret data (D)
- Knowledge of any pieces (k-1) makes secret data (D) completely undetermined.

Such a scheme is called a (k,n) threshold scheme

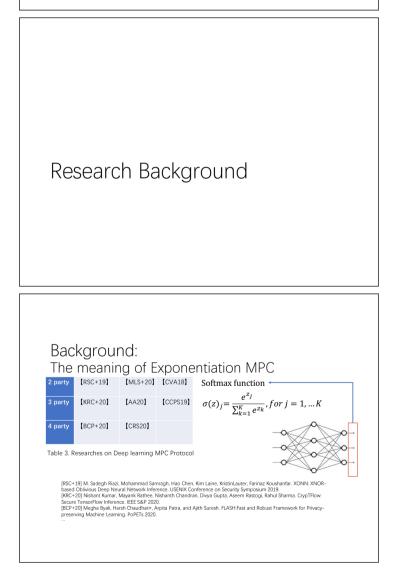
Variants of Secret Sharing Scheme

 $\begin{array}{ll} \text{Shamir' s Secret Sharing} \\ s \text{ is secret} \\ f(x) = a_{t-1}x^{t-1} + \cdots + a_1x + a_0 \\ a_0 = s, \\ select \ a_i(i = 1, \ldots, t) \ randomly \\ share \ s_i = f(i) \ (i = 1, \ldots, n) \end{array} \qquad \begin{array}{l} \text{Additive Secret Sharing} \\ x \in \mathbb{G} \ is secret \\ x_1 + \cdots + x_n \equiv x \ mod \ p \\ share \ x_i \in \mathbb{G} \ , (i = 1, \ldots, n) \end{array}$

	Threshold	Set	Core Technique
Shamir's Secret Sharing	k <n 2<="" td=""><td>\mathbb{F}_p (p: prime)</td><td>Lagrange interporation</td></n>	\mathbb{F}_p (p: prime)	Lagrange interporation
Additive Secret Sharing	n-1	G (Finite Additive Group)	



		Addition and Multiplication in MPC				
Party 1 generates [<i>a</i>] Party 2 generates [<i>b</i>]						
		formulation	Communication			
	Addition	[a] + [b] = [a+b]	Local (0 round)			
	Multiplication	$[a] \cdot [b] = [a \cdot b]$	1 round			
	general, all of th lition and multi	e computations are impl plication.	emented by using			

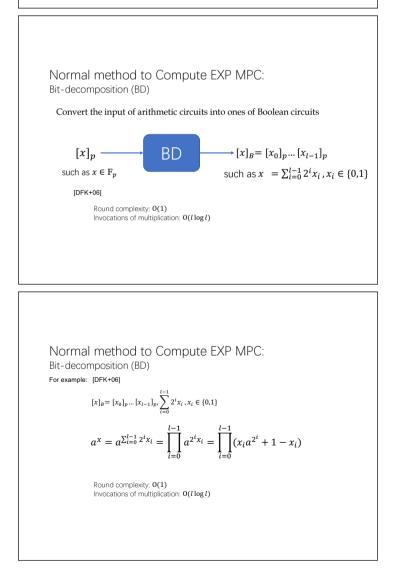


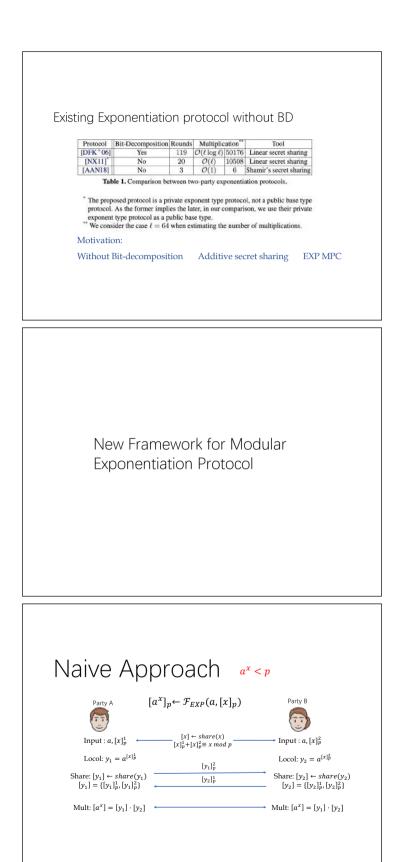
Background: 3 types of Exponentiation MPC

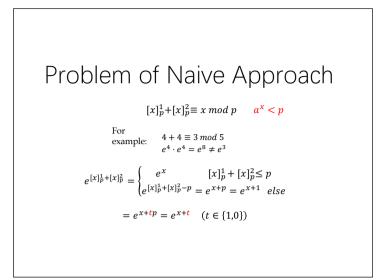
Public Base: a^[x]
Public Exponent: [a]^x
Private Exponentiation: [a]^[x]

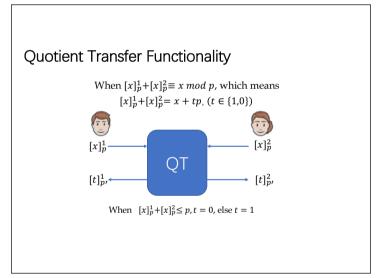
Our work consider the setting public base

$$\sigma(z)_j = \frac{e^{z_j}}{\sum_{k=1}^K e^{z_k}}, for j = 1, \dots K$$





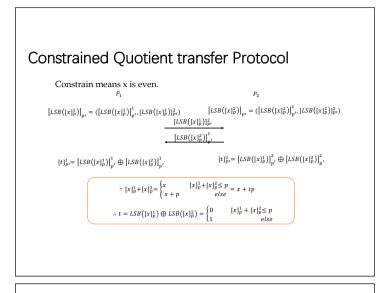




Constrained Quotient transfer Protocol

Constrain means x is even.

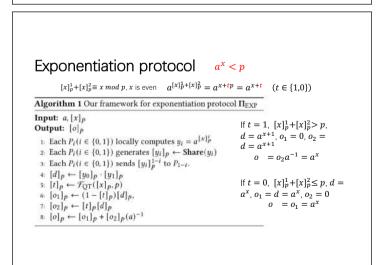
 $\begin{aligned} x &= 4, p = 7, p' = 11\\ [x]_7^1 + [x]_7^2 = 4mod \ 7\\ [x]_7^1 &= 5 \qquad [x]_7^2 = 6\\ &\because [x]_7^1 + [x]_7^2 = 11 > 7 \qquad \therefore t = 1\\ [LSB([x]_7^1)]_{11} &= 1 \qquad [LSB([x]_7^2)]_{11} = 0\\ &[LSB([x]_7^1)]_{11} + [LSB([x]_7^2)]_{11}\\ &- 2 \times [LSB([x]_7^2)]_{11} \times [LSB([x]_7^2)]_{11} = 1 \end{aligned}$



Constrained Quotient transfer Protocol

Algorithm 3 Our Constrained Quotient Transfer Protocol Π_{QT}

Input: $[x]_{p,p'}$ Output: $[t]_{p'}$ 1: Each $P_i(i \in \{0,1\})$ computes $b_i = \text{LSB}([x]_{p}^i)$. 2: Each $P_i(i \in \{0,1\})$ computes $[b_i]_{p'} \leftarrow \text{Share}(b_i,p')$. 3: Each $P_i(i \in \{0,1\})$ sends $[b_i]_{p'}^{1-i}$ to P_{1-i} . 4: $[t]_{p'} = [b_0]_{p'} + [b_1]_{p'} - 2 \cdot [b_0]_{p'} \cdot [b_1]_{p'}$ 5: Output $[t]_{p'} = ([t]_{p'}^{0}, [t]_{p'}^{1})$



Problem 2 : assumption

 $a^x = \sqrt{a}^{2x}$

 \sqrt{a} dose not always exist in \mathbb{Z}_p

We need b and p, which satisfy

 $a = b^2 \mod p'$ $a^x < p'$

Assume we can find such b and p'

Conversion protocol

 $[x]_{p} \leftarrow [x]_p$

Algorithm 2 Our modulus conversion protocol IIConv

- Input: $[x]_p, p'$ $\begin{array}{l} \text{Input: } [x]_{p'} \\ \text{Output: } [x]_{p'} \\ 1: [t']_{p'} \leftarrow \mathcal{F}_{\text{QT}}([x]_{p}, p') \\ 2: \text{ Each } P_i(i \in \{0, 1\}) \text{ sets } [x]_{p'}^i = [x]_p^i - [t']_{p'}^i \cdot p \end{array}$
- 3: Output [x]_{p'}

Correctness

$$[x']_{p'}^{i} = [x]_{p}^{i} - [t]_{p'}^{i} \times p$$

$$[x']_{p'}^{1} = [x]_{p}^{1} - [t]_{p'}^{1} \times p \qquad [x']_{p'}^{2} = [x]_{p}^{2} - [t]_{p'}^{2} \times p$$

$$[x']_{p'}^{1} + [x']_{p'}^{2} \mod p' = [x]_{p}^{1} - [t]_{p'}^{1} \times p + [x]_{p}^{2} - [t]_{p'}^{2} \times p \mod p'$$

$$= [x]_{p}^{1} + [x]_{p}^{2} - ([t]_{p'}^{1} + [t]_{p'}^{2}) \times p \mod p'$$

$$= x + t \times p - ([t]_{p'}^{1} + [t]_{p'}^{2}) \times p \mod p'$$

Correctness

$$[x']_{p'}^{1} + [x']_{p'}^{2} \mod p' = x + t \times p - \left([t]_{p'}^{1} + [t]_{p'}^{2}\right) \times p \mod p'$$

$$\begin{bmatrix} x + t \times p - t \times p \mod p' = x \quad [t]_{p'}^{1} + [t]_{p'}^{2} < p' \\ x + t \times p - (t + p') \times p \mod p' \quad \text{else} \\ x \end{bmatrix}$$

Our Exponentiation Protocol

Algorithm 4 Our concrete exponentiation protocol Π'_{EXP}

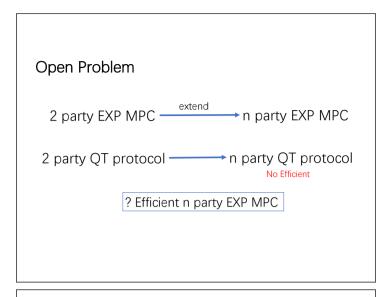
Input: $a, [x]_p, p'$ Output: [o]p' 1: $b := \sqrt{a}$, where $b \in \mathbb{Z}_{p'}$ 1: $p := \forall a$, where $v = \neg_p$ 2: $[2x]_p \leftarrow 2[x]_p$ 3: if $p \neq p'$ then 4: $[2x]_{p'} \leftarrow \Pi_{\text{Conv}}([2x]_p, p')$ 5: $v := [2x]_{p'}$ 6: else 7: $v := [2x]_p$ 8: end if 9: Output $[o]_{p'} \leftarrow \Pi_{\text{EXP}}(b, v)$

Our Result

Protocol	BD	Rounds	Multiplic	ation [†]	Tool	Dishonest-Majority
[DFK ⁺ 06]	Yes	119	O(tlogt)	50176	Linear secret sharing	No
[NX11]*	No	20	O(t)	10508	Linear secret sharing	No
[AAN18]	No	3	O(1)	6	Shamir's secret sharing	No
This work (with conversion)5	No	6	O(1)	4	Additive secret sharing	Yes
This work (w/o conversion)\$	No	- 4	O(1)	3	Additive secret sharing	Yes

Table 1: Comparison between two-party exponentiation protocols.

* The proposed portocel is a private exponent type protocol, not a public base type protocol. As the former implies the later, in our comparison, we use their private exponent type portocel as a public base type. ¹ We consider the case 4 = 64 when estimating the number of multiplications.
³ Here, we consider two cases whether we need a modulus conversion. As mentioned in Section 1.3, in our protocol, if the public base does not have quadratic residue, we require an additional modulus conversion process. In this code, when our modulus conversion is used, we need additioned 2 rounds and 1 motional or during the number of the public base does not have quadratic residue, we require an additional modulus conversion process. In this code, when our modulus conversion is used, we need additioned 2 rounds and 1 motional or during the number of the public base does not have quadratic residue, we require an additional modulus conversion process.



Thank you for your listening

November 8–10, 2021, Kyushu University

General-purpose Compiler for Secure Three-party Computation and Its Application to Prediction by Machine Learning Model

Hikaru Tsuchida

NEC Corporation h_tsuchida@nec.com

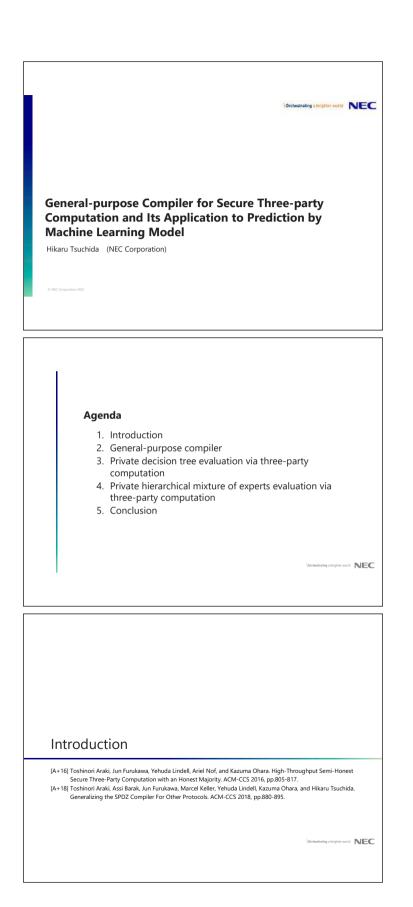
Multiparty computation (MPC) based on a secret sharing scheme (SS-MPC) enables multiple parties to compute an arbitrary function represented as a circuit without revealing parties' inputs. In SS-MPC, each party distributes its inputs as *shares* that look like random numbers among several parties, and the computation proceeds by using shares locally and communicating among the parties. In particular, the secure threeparty computation protocol based on a replicated secret sharing scheme (SS-3PC) over the ring [1] has gained attention in recent years because it can perform high throughput even when SS-3PC computes a complex function (e.g., machine learning applications) represented as mixed circuits (which are composed of Boolean and arithmetic circuits). When SS-MPC computes a complex function represented as mixed circuits, efficient share conversion protocols can improve performance. In particular, SS-3PC over \mathbb{Z}_{2^k} can achieve faster share conversions than that over the prime-order field because \mathbb{Z}_{2^k} preserves the structure of the individual bits more than the prime-order field.

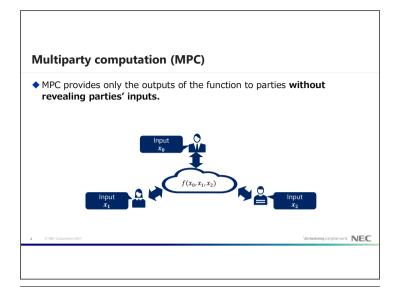
While research on protocol design is ongoing, there is still a significant obstacle to implement the applications via MPC due to the high level of expertise required to design a specific MPC execution considering a trade-off between communication and round complexities. Research and development of general-purpose compilers have been actively conducted to mitigate this problem. It can compile the high-level codes to the mixed circuits that MPC computes. Hence, by using the general-purpose compilers, even non-experts of MPC can implement applications based on MPC.

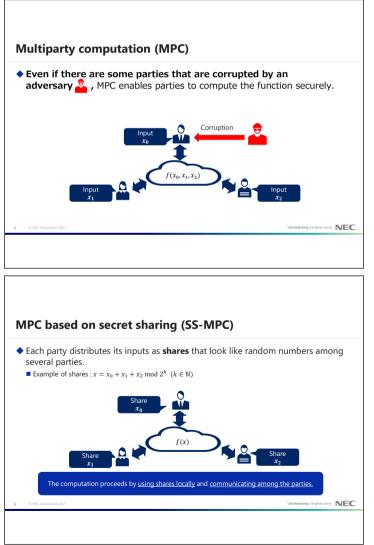
In this talk, we explain one of the general-purpose compilers for SS-3PC, *NEC-SPDZ* and the share conversion protocols over \mathbb{Z}_2 and \mathbb{Z}_{2^k} to compute a complex function via SS-3PC by referring to [2]. We also explain the implementation based on NEC-SPDZ and evaluation of the prediction by typical machine learning models, e.g., the decision tree and the hierarchical mixture of experts models via SS-3PC by referring to [2, 3].

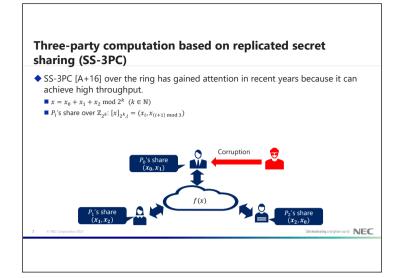
References

- Toshinori Araki, Jun Furukawa, Yehuda Lindell, Ariel Nof, and Kazuma Ohara. High-Throughput Semi-Honest Secure Three-Party Computation with an Honest Majority. ACM-CCS 2016, pp.805-817.
- [2] Toshinori Araki, Assi Barak, Jun Furukawa, Marcel Keller, Yehuda Lindell, Kazuma Ohara, and Hikaru Tsuchida. Generalizing the SPDZ Compiler For Other Protocols. ACM-CCS 2018, pp.880-895.
- [3] Yusaku Maeda, Hikaru Tsuchida, Kazuma Ohara, Ryo Furukawa, Isamu Teranishi, and Koji Nuida. Implementation and Evaluation of Prediction by Heterogeous Mixture Models based on Three-Party Secure Computation. SCIS 2020, 3C3-5.

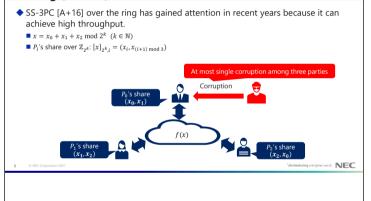




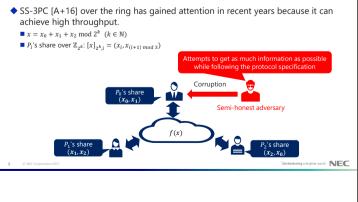


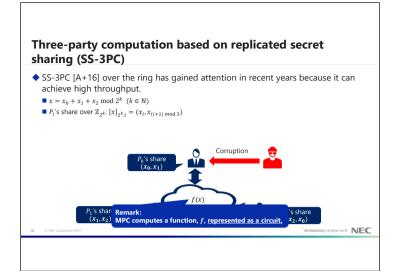


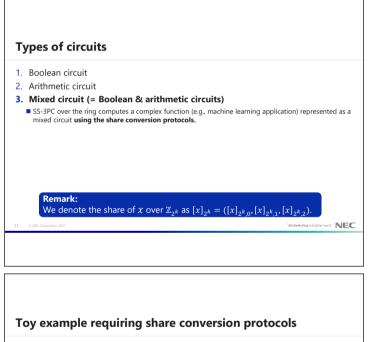
Three-party computation based on replicated secret sharing (SS-3PC)

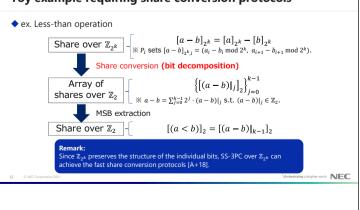


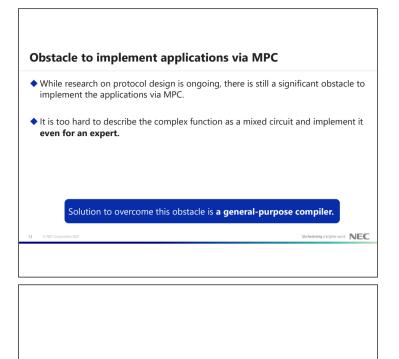
Three-party computation based on replicated secret sharing (SS-3PC)











General-purpose compiler

[A+18] Toshinori Araki, Assi Barak, Jun Furukawa, Marcel Keller, Yehuda Lindell, Kazuma Ohara, and Hikaru Tsuchida. Generalizing the SPDZ Compiler For Other Protocols. ACM-CCS 2018, pp.880-895.

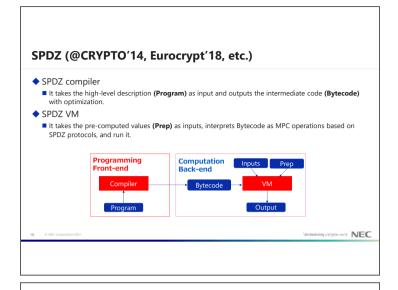
Orchestrating a brighter world NEC

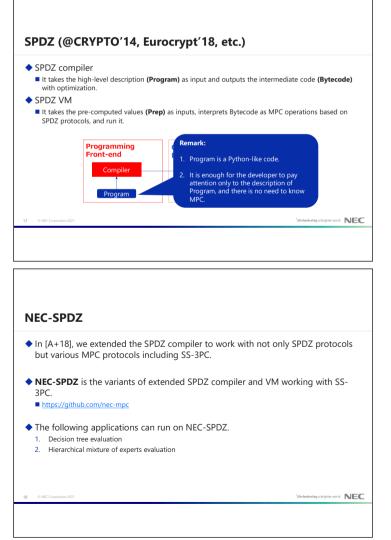
NEC

General-purpose compiler

 General-purpose MPC compiler can compile the high-level descriptions into the MPC operations based on various MPC protocols.

- Ex) SPDZ (also known as SCALE-MAMBA), MP-SPDZ, Obliv-C, ...
- Researchers and developers around the world are interested in the generalpurpose compiler.
- SoK paper in IEEE S&P'19 • HASTINGS, Marcella, et al. SoK: General purpose compilers for secure multi-party computation. In: 2019 IEEE symposium on security and privacy (SP). IEEE, 2019. p. 1220-1237.
- Contributed talk in RWC'20 • https://rwc.iacr.org/2020/slides/Hastings.pdf





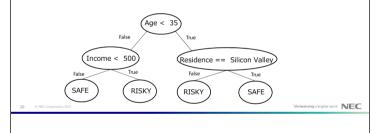
Private decision tree evaluation via three-party computation

[A+18] Toshinori Araki, Assi Barak, Jun Furukawa, Marcel Keller, Yehuda Lindell, Kazuma Ohara, and Hikaru Tsuchida. Generalizing the SPDZ Compiler For Other Protocols. ACM-CCS 2018, pp.880-895.

\Orchestrating a brighter world NEC

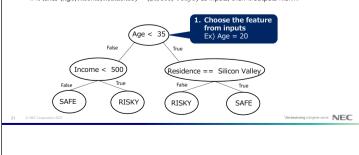
Decision tree

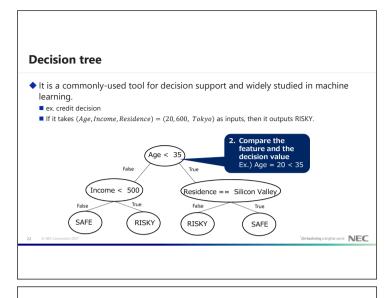
- It is a commonly-used tool for decision support and widely studied in machine learning.
 - ex. credit decision
 - If it takes (Age, Income, Residence) = (20, 600, Tokyo) as inputs, then it outputs RISKY.

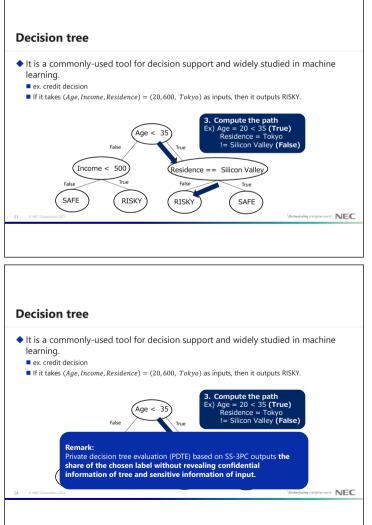


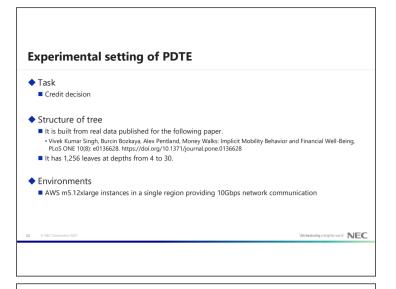
Decision tree

- It is a commonly-used tool for decision support and widely studied in machine learning.
 ex. credit decision
- If it takes (*Age*, *Income*, *Residence*) = (20, 600, *Tokyo*) as inputs, then it outputs RISKY.

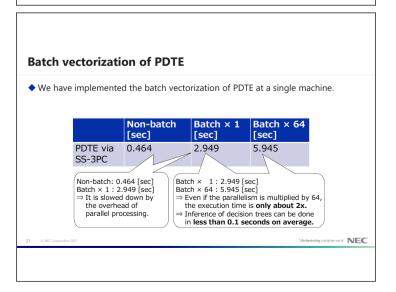








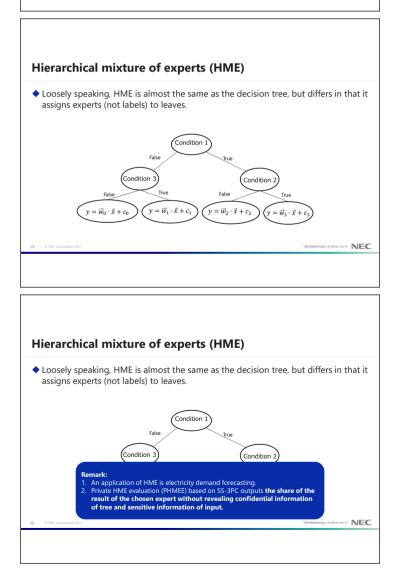
Single execution of PDTE The execution time of PDTE via SS-3PC is shorter than that via the other MPC protocols. SS-3PC BMR (※1) Resource SPD7 [LN17] (\mathbb{Z}_{2^k}) Security (n: # parties t: # corruptions) Semi-Malicious Malicious Malicious honest (※2) (※2) (※2) ∞2) t<n t < n/2t < n t < n/2Online time 1 core 0.4641 0.3005 3.0416 0.5353 [sec] 2746 # rounds 783 584 28 (Not 5.2204 (Not 1041.8 Pre-48 cores computation time [sec] required) (%3) required) %1_BMR tan on I3_2Marge instances. %2_ The malicious security is stronger than the semi-honest security. %3_ It ran on 48 Marge instances [UNT] Lindet Yehuda, and Arel Not TA framework for constructing last MPC over arithmetic circuits with malicious adversaries and an honest-majority." Proceedings of the 2017 ACM SIGAC Conference on Computer and Communications Security. 2017. Orchestration a brinklas NEC

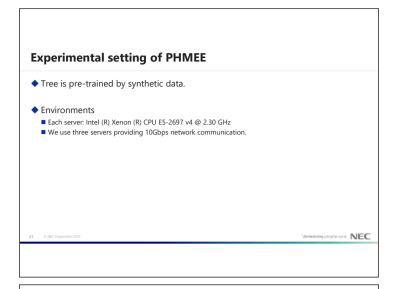


Private hierarchical mixture of experts evaluation via three-party computation

[M+20] Yusaku Maeda, Hikaru Tsuchida, Kazuma Ohara, Ryo Furukawa, Isamu Teranishi, and Koji Nuida. Implementation and Evaluation of Prediction by Heterogeneous Mixture Models based on Three-Party Secure Computation. SCIS 2020, 32-5.

\Orchestrating a brighter world NEC

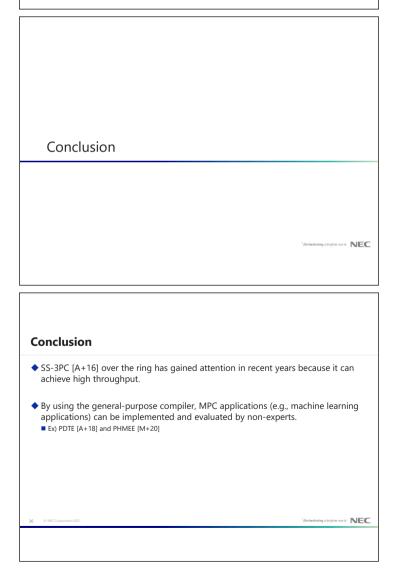




ht of tree	: 4				
ber of input dat	Execution time [sec]				
of input vector	plaintext	MPC (fixed-point number)	MPC (floating-point number)		
1	4.23×10^{-5}	1.68×10^{-1}	1.61		
2	4.27×10^{-5}	2.22×10^{-1}	2.36		
3	4.54×10^{-5}	2.97×10^{-1}	3.51		
4	4.88×10^{-5}	3.43×10^{-1}	4.10		
5	5.11×10^{-5}	3.88×10^{-1}	5.06		

mension of input nber of input dat				
Height of tree		Execution time [s		
	plaintext	MPC (fixed-point number)	MPC (floating-point number)	
2	3.64×10^{-5}	6.91×10^{-2}	8.56×10^{-1}	
3	$3.88 imes 10^{-5}$	1.32×10^{-1}	1.56	
4	4.55×10^{-5}	2.97×10^{-1}	3.51	
5	$5.12 imes 10^{-5}$	4.88×10^{-1}	5.25	
6	5.86×10^{-5}	9.52×10^{-1}	11.8	

# dimension of inpu Height of tree	: 3					
Number of input		Execution time [sec]				
data	plaintext	MPC (fixed-point number)	MPC (floating-point number)			
1	8.87×10^{-6}	3.47×10^{-2}	4.65×10^{-1}			
10	4.55×10^{-5}	2.97×10^{-1}	3.51			
20	1.10×10^{-5}	$4.57 imes 10^{-1}$	5.51			
30	1.67×10^{-5}	$5.05 imes 10^{-1}$	7.36			
40	1.79×10^{-5}	8.47×10^{-1}	11.6			
Remark: As the numb	er of input data incre		cution time over MPC			





November 8-10, 2021, Kyushu University

Evolving Secret Sharing From Evolving Perfect Hash Families

Kirill Morozov

University of North Texas Kirill.Morozov@unt.edu

The concept of Evolving Secret Sharing introduced by Komargodski, Naor and Yogev [4] puts forward an idea of maintaining secret sharing schemes with potentially infitine number of participants. Specifically, in this framework, new shares are generated for new participants on demand, and no communication with old participants is required.

Armed with the relation between perfect hashing families (PHF) and secret sharing schemes [2, 1, 5], we introduce an evolving (non-abelian) multiplicative secret sharing scheme. An importance of secret sharing over non-abelain groups is that it encompasses, e.g., permutation groups—a basis for MIX operations used, in particular, in electronic voting.

To achieve our goal, we introduce a novel concept of Evolving PHF. In these families, a domain of the hash function is not known in advance, but may be increased in the future—according to a particular application. The framework of Evolving PHF may be of independent interest, and it may encompass other combinatorial objects.

This talk is based on a joint work with Yvo Desmedt and Sabyasachi Dutta [3].

References

- Blackburn, S. R., Burmester, M., Desmedt, Y. and Wild, P. R., "Efficient multiplicative sharing schemes", Eurocrypt '96, LNCS 1070, 107-118 (1996)
- [2] Desmedt, Y., Di Crescenzo, G. and Burmester, M., "Multiplicative Non-abelian Sharing Schemes and their Application to Threshold Cryptography", Asiacrypt '94: 21-32 (1994)
- [3] Desmedt, Y., Dutta, S., Morozov, K. "Evolving Perfect Hash Families: A Combinatorial Viewpoint of Evolving Secret Sharing", CANS 2019: 291-307 (2019)
- [4] Komargodski, I., Naor, M. and Yogev, E., "How to Share a Secret, Infinitely", TCC (B2) 2016: 485-514 (2016)
- [5] Safavi-Naini R., Wang H., "Robust Additive Secret Sharing Schemes over Z_m . Cryptography and Computational Number Theory. Progress in Computer Science and Applied Logic, vol 20: 357-368, Birkhauser (2001)



Evolving Secret Sharing From Evolving Perfect Hash Families

Kirill Morozov (諸蔵 霧流) University of North Texas

IMI Workshop of the Joint Research Projects

Exploring Mathematical and Practical Principles of Secure Computation and Secret Sharing

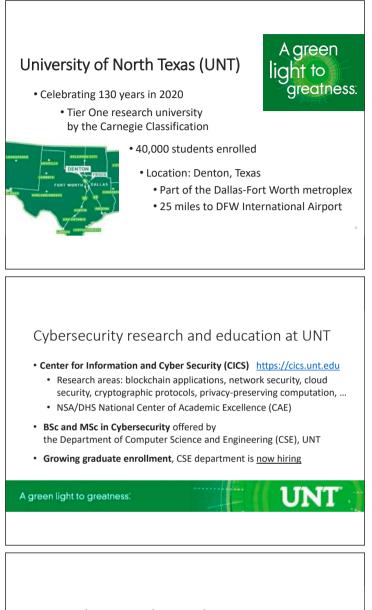
November 9, 2021

Credits

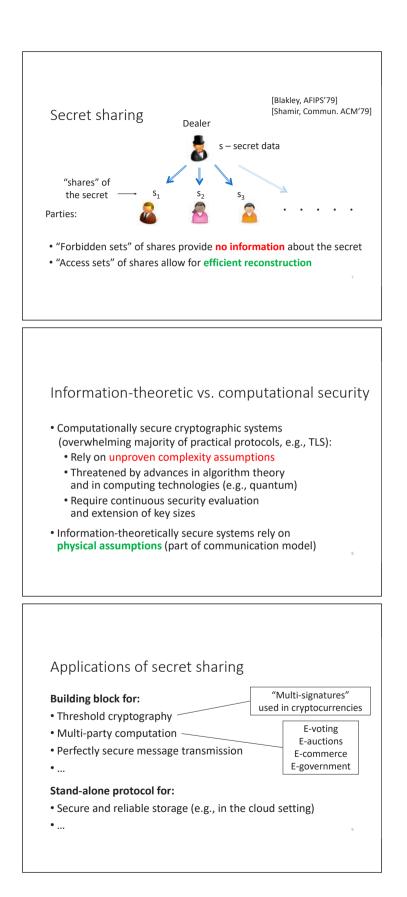
• This presentation is based on a joint work with Yvo Desmedt (University of Texas at Dallas) and Sabyasachi Dutta (University of Calgary), published at CANS 2019

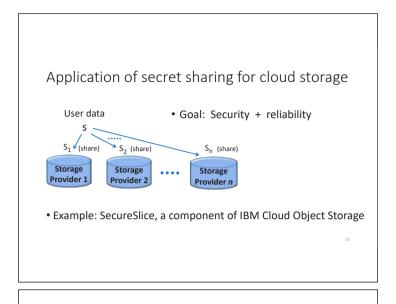
Plan of this talk

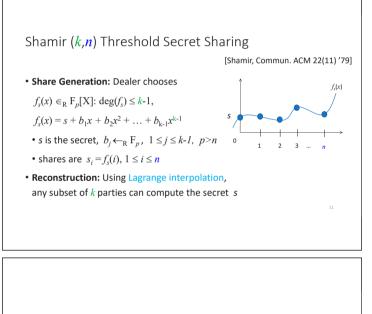
- Short introduction of UNT
- Secret sharing and its applications
- Evolving secret sharing (Komargodski, Naor, Yogev, TCC 2016)
- Secret sharing from perfect hashing (multiplicative scheme)
- Evolving perfect hash families: definition and construction
 - Implication for secret sharing
- Conclusion and future works



Secret sharing and its applications







Example application: Long-term storage

- As new storage providers emerge and old ones go out of business, it would be convenient for the data owner (dealer) to keep adding providers (parties) on the rolling basis
- Problem: Scalability, as we need p > # parties for Shamir's scheme
- What if the number of parties is not known in advance?
 - E.g., potentially infinite
- May choose a large "p" but still cannot support infinitely many parties

Solutions

- [Cachin '95], [Csirmaz and Tardos, '12]: On-line secret sharing • # of authorized sets a party can join is bounded
- [Komargodski, Naor, Yogev '16]: Evolving secret sharing
 - More efficient, no limitation as above
 - Many follow-up works

Comparison of secret sharing protocols

- Secret redistribution (Wong, Wing, Wang '02): The parties change access structure <u>without involving the dealer</u> (e.g., enroll new members)
 - Note: No secret reconstruction is done
- Evolving secret sharing: The dealer adds parties on demand
 - Note: The dealer knows the secret (or can reconstruct it using existing parties)

Evolving secret sharing (KNY16)

- General evolving access structures: The size of T-th participant's share is 2^{T-1}
- Evolving k-threshold's share size: $\sigma'(T) = \log T + (k-1) \cdot max \{ \log T + k , \sigma(\log T + k) \},$ where the share size of the base scheme is $\sigma(t)$
 - When Shamir secret sharing is the base scheme
- Let us consider this construction for k=2
 - (Any two parties can reconstruct the secret)

$KNY16 (2,\infty)-threshold scheme$ $Secret s \in GF(p); \quad b_i \leftarrow_R GF(p)$ Divide parties in "generations"; gen. g has Size(g) = 2^g $Party T belongs to generation g = \lfloor \log T \rfloor$ $(k,n)-threshold Shamir sharing of s \in GF(p) is denoted by Sh(k,n)(s)$ $Gen 0 : P_1 [b_1]$ $Gen 1 : P_2 [s+b_1, b_2, Sh_1(2,2)(s)]; P_3 [s+b_1, b_2, Sh_1(2,2)(s)]$ $Gen 2 : P_4 [s+b_1, s+b_2, b_3, Sh_2(2,4)(s)]; P_5 [s+b_1, s+b_2, b_3, Sh_2(2,4)(s)]$ $P_6 [s+b_1, s+b_2, b_3, Sh_2(2,4)(s)]; P_7 [s+b_1, s+b_2, b_3, Sh_2(2,4)(s)]$

$(2,\infty)$ -threshold scheme: Correctness and security (sketch) Gen 0 : P₁ [b₁]

```
 \begin{array}{l} {\rm Gen} \ 1 \ : \ P_2 \ \left[ \ s + b_1 \, , \, b_2 \, , \, Sh_1(2,2)(s) \ \right] \ ; \ P_3 \ \left[ \ s + b_1 \, , \, b_2 \, , \, Sh_1(2,2)(s) \ \right] \\ {\rm Gen} \ 2 \ : \ P_4 \ \left[ \ s + b_1 \, , \, s + b_2 \, , \, b_3 \, , \, Sh_2(2,4)(s) \ \right] \ ; \ P_5 \ \left[ \ s + b_1 \, , \, s + b_2 \, , \, b_3 \, , \, Sh_2(2,4)(s) \ \right] \\ {\rm P_6 \ \left[ \ s + b_1 \, , \, s + b_2 \, , \, b_3 \, , \, Sh_2(2,4)(s) \ \right] \ ; \ P_7 \ \left[ \ s + b_1 \, , \, s + b_2 \, , \, b_3 \, , \, Sh_2(2,4)(s) \ \right] \\ \end{array} \right.
```

- Reconstruction: Gen 0 (P_1) uses b_1 with any party down the generations

- Security: One-time pad (p-ary)
- Reconstruction: Gen 1: Within the same generation, use Shamir's share, down the generations, use ${\rm b_2}$
- Security: Within the same generation, Shamir's scheme
 down the generations, one-time pad

(2,∞)-threshold scheme: Correctness and security (sketch), cont.

```
Gen 0: P<sub>1</sub> [b<sub>1</sub>]
Gen 1: P<sub>2</sub> [s+b<sub>1</sub>, b<sub>2</sub>, Sh<sub>1</sub>(2,2)(s)]; P<sub>3</sub> [s+b<sub>1</sub>, b<sub>2</sub>, Sh<sub>1</sub>(2,2)(s)]
Gen 2: P<sub>4</sub> [s+b<sub>1</sub>, s+b<sub>2</sub>, b<sub>3</sub>, Sh<sub>2</sub>(2,4)(s)]; P<sub>5</sub> [s+b<sub>1</sub>, s+b<sub>2</sub>, b<sub>3</sub>, Sh<sub>2</sub>(2,4)(s)]
P<sub>6</sub> [s+b<sub>1</sub>, s+b<sub>2</sub>, b<sub>3</sub>, Sh<sub>2</sub>(2,4)(s)]; P<sub>7</sub> [s+b<sub>1</sub>, s+b<sub>2</sub>, b<sub>3</sub>, Sh<sub>2</sub>(2,4)(s)]
To continue, apply the same reasoning as in the previous slide, recursively
Reconstruction: Gen 2: Within the same generation, use Shamir's share, down the generations, use b<sub>3</sub>
Security: Within the same generation, Shamir's scheme down the generations, one-time pad
```

Discussion

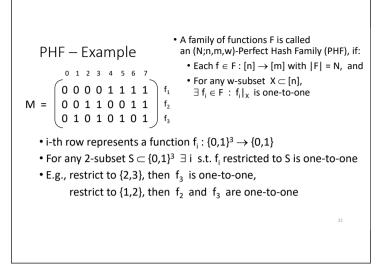
- A (k,∞)-threshold scheme was also presented in [KNY16]
 Out of scope today
- For the above $(2,\infty)$ -threshold scheme, we need to work over a field (because Shamir's scheme is used)

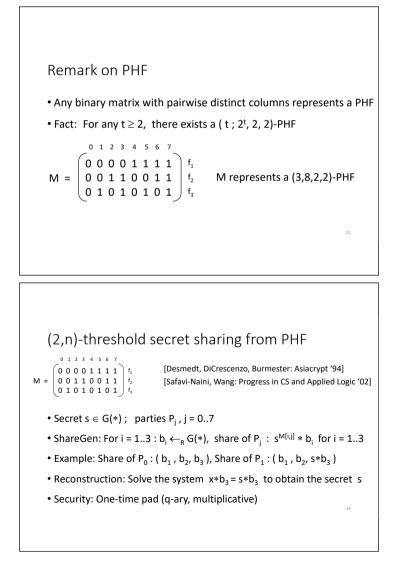
Our goals

- Understand combinatorial interpretation of evolving secret sharing schemes
- Avoid the use of finite fields
 - To accommodate the most general case, e.g., a permutation group (which is non-abelian)

Perfect hash family - Definition

- A family of functions F is called an (N;n,m,w)-Perfect Hash Family (PHF), if:
 - Each $f \in F: [n] \rightarrow [m]$ with |F| = N, and
 - \bullet For any w-subset $\, X \subset [n], \, \exists \, g \in F \, : \, g \big|_X \,$ is one-to-one





(2,n)-threshold secret sharing from PHF (cont.)

 $\mathsf{M} = \begin{pmatrix} \begin{smallmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 \end{pmatrix} \begin{pmatrix} \mathsf{f}_1 \\ \mathsf{f}_2 \\ \mathsf{f}_3 \end{pmatrix} \bullet \begin{array}{l} \mathsf{Secret} \ \mathsf{s} \in \mathsf{G}(*) \ ; \ \mathsf{parties} \ \mathsf{P}_j \ ; \ \mathsf{g} = 0..7 \\ \bullet \ \mathsf{ShareGen:} \ \mathsf{For} \ i = 1..3 \ : \ \mathsf{b}_i \leftarrow_{\mathsf{R}} \ \mathsf{G}(*) \\ \bullet \ \mathsf{Share of} \ \mathsf{P}_j \ : \ \mathsf{S}^{\mathsf{M}[i,j]} \ast \ \mathsf{b}_i \ \ \mathsf{for} \ i = 1..3 \\ \bullet \ \mathsf{Share of} \ \mathsf{P}_j \ : \ \mathsf{S}^{\mathsf{M}[i,j]} \ast \ \mathsf{b}_i \ \ \mathsf{for} \ i = 1..3 \\ \bullet \ \mathsf{Share of} \ \mathsf{P}_j \ : \ \mathsf{Share of} \ \mathsf{P}_j \ : \ \mathsf{Share of} \ \mathsf{P}_j \ : \ \mathsf{Share of} \ \mathsf{Share$

- In general: Reconstruction follows by the w-subset (last) property of PHF
- Question: Can we construct an evolving scheme?
- Natural approach: "Evolving" PHF

Preliminary definitions

- Def.: Evolving family of sets: A sequence of sets $\{X_n\}_{n\geq 0}$ is an evolving family of sets if $X_i \subset X_{i+1}$ for all $i\geq 0$, i.e., the family is strictly monotone increasing
- Def. (Partial function): A rule $X \to Y$ is called a partial function, if there exists a subset $X' \subset X$ s.t. when restricted to X', $f|_{X'}: X' \to Y$ is a (total) function

Evolving Perfect Hash Functions – Definition

- Def.: Let {X_r} be an evolving family of sets, {Y_r} be a sequence of sets (which may or may not be evolving) and {w_r} be a non-decreasing sequence of positive integers
 - A sequence of families of partial and total functions $\{\mathcal{F}_r\}$ is called an ($\{X_r\}, \{Y_r\}, \{w_r\}$)-Evolving PHF, if:
 - + Each $f\in \mathcal{F}_r$ is a partial/total function from $X_r\!\rightarrow\!Y_r$ and
 - For any w_r -subset $X' \subset X_r$, there exists $g \in \mathcal{F}_r$ such that the restriction of g of X' is one-to-one

Remarks

- In the paper, we make a distinction between "evolving" PHF family, which is finite and "perpetually evolving", which is infinite
- In such the families, only the sequence of domains $\{X_r\}$ needs to be an evolving family of sets
- The sequence of co-domains {Y_r} need not be evolving, in fact, it can be constant, i.e., Y_r = Y for all r
- In addition, the non-decreasing sequence of $\{w_r\}$ can be a constant sequence

Our proposal of Perpetually Evolving PHF

- Focus on the binary case, i.e., co-domain Y_r = Y = {0,1} and w_r = w = 2, for all r
- Notation: An m-dimensional vector of zeroes as $\mathbf{0}_{\rm m}$ and that of ones as $\mathbf{1}_{\rm m}$
 - After introduction of r-th partial row, the evolved matrix is denoted as M(r)
 - Denote the non-zero columns of M as C₁,...,C_{2^t-1}
 - Each of them is a t-bit column vector

Our construction

- Consists of the following three procedures:
- Init: Assign 0_t as the first column of M(0)
- 1st Partial Row:
 - 1. Place the remaining $2^{t}-1$ columns $C_{1},...,C_{2^{t}-1}$ to the right of 0_{t}
 - 2. Append a partial row $0_{2^{t}-1}$ just below them
 - 3. Copy $C_1, ..., C_{2^{t}-1}$ to the right as columns $2^{t}+1$ to $2^{t+1}-1$
 - 4. Append a partial row $1_{2^{t}.1}$ just below the columns copied above

Our construction (cont.)

• r-th Partial Row to M(r-1):

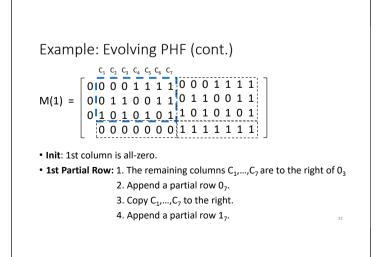
- 1. Choose the last a = $\lceil \alpha/2 \rceil$ columns B[1], B[2], ..., B[a] of M(r-1), where α denotes # columns in M(r-1)
- 2. Append a partial row 0_a just below B[1], B[2], ..., B[a]
- 3. Copy B[1], B[2], ..., B[a] to the right of M(r-1)
- 4. Append a partial row 1_a just below the columns copied above

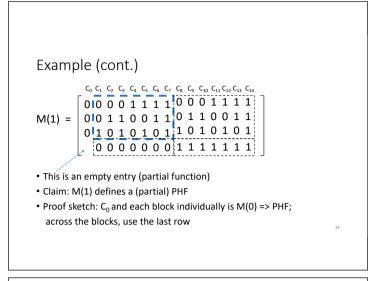
Example: Evolving PHF

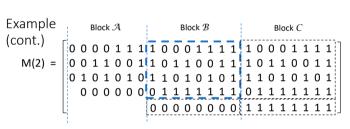
$$M(0) := M = \begin{pmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 \end{pmatrix}$$

• Let us with a PHF defined by M

- Denote it as M(0)
- Next, let us compute the next generation M(1)







• Claim: M(2) defines a (partial) PHF

- Consider the blocks of columns $\mathcal{A}\text{, }\mathcal{B}\text{ and }C\text{ as marked above }$

- Any pair of columns in Blocks ${\mathcal B} \, {\rm and} \, {\mathcal C} \, {\rm differ}$ in at least position due to the last row

• Any pair of columns in Block A and Block B (resp. Block C) differ in at least one position because M(1) is PHF

Main result

- Thm.: Our construction implements a perpetually evolving PHF.
- Proof (sketch): By induction.
 - The base case intuition: two slides back.
 - The induction step intuition: the previous slide.
- \bullet Corollary: There exists an evolving (2, ∞)-threshold multiplicative secret sharing scheme
- Note: The underlying group may be non-abelian

Parameters and share size

- If the 1st column of M(0) is t-dimensional, r-th partial row adds
 [(3/2)⁻¹2^t] new columns, i.e., increases the domain by
 exponentially many elements
- Share size for T-th participant: (t + O(log(r,T)))·log|G|

Conclusion

- Studied a combinatorial interpretation of evolving secret sharing
- Proposed a recursive construction of perpetually evolving PHF
 It implies an evolving (2,∞)-threshold multiplicative secret sharing scheme

Future work

- Further study of evolving combinatorial objects
 - Blueprint: Start with a recursive construction for such, and develop it into an evolving scheme
- Extension to (k, ∞)-threshold case

References

- 1. Blakley, G.R.: Safeguarding cryptographic keys. AFIPS 1979.
- 2. Cachin, C.: On-line secret sharing. Cryptography and Coding, 1995.
- 3. Csirmaz, L., Tardos, G.: On-line secret sharing. Des. Codes Crypt. 63(1), 2012.
- Desmedt, Y., Di Crescenzo, G., Burmester, M.: Multiplicative non-abelian sharing schemes and their application to threshold cryptography. ASIACRYPT 1994.
- Desmedt, Y., Dutta, S., Morozov, K.: Evolving Perfect Hash Families: A Combinatorial Viewpoint of Evolving Secret Sharing, CANS 2019.
- 6. Komargodski, I., Naor, M., Yogev, E.: How to share a secret, infinitely. TCC 2016.
- Safavi-Naini, R., Wang, H.: Robust additive secret sharing schemes over Zm. Cryptography and Computational Number Theory. Progress in Computer Science and Applied Logic (20), 2001.
- 8. Shamir, A.: How to share a secret. Commun. ACM 22(11), 1979.
- Wong, T. M., Wang, C., and Wing, J. M.: Verifiable secret redistribution for archive system," IEEE Security in Storage Workshop, 2002.



Thank you very much for your attention, and questions, please!

(Kirill.Morozov@unt.edu)

November 8–10, 2021, Kyushu University

Secure-Computation AI : a Python Library for Machine Learning in Secure Computation

Ibuki Mishina (Joint work with Dai Ikarashi, Koki Hamada and Ryo Kikuchi)

> NTT Corporation ibuki.mishina.br@hco.ntt.co.jp

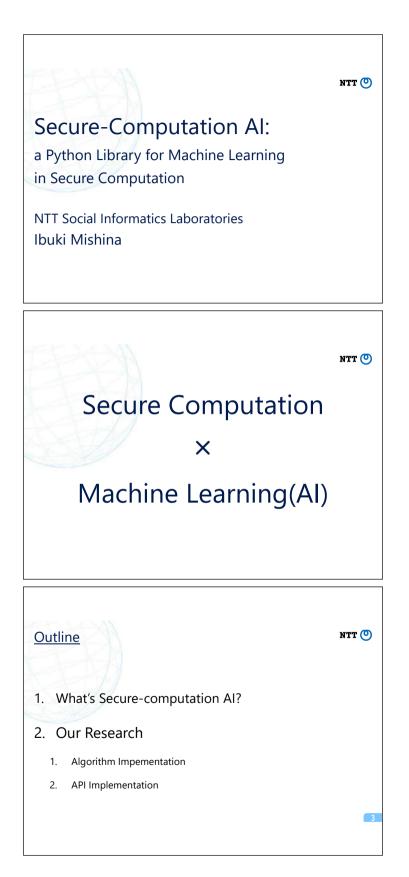
Big data analysis using machine learning (AI) is expected to be a technology that enables complex analysis and inference, but because it requires a large amount of data, including personal information, it often faces issues related to privacy. Therefore, as a solution to this problem, a technology has been attracting attention in recent years, in which learning and inference is calculated while keeping data encrypted using secure computation.

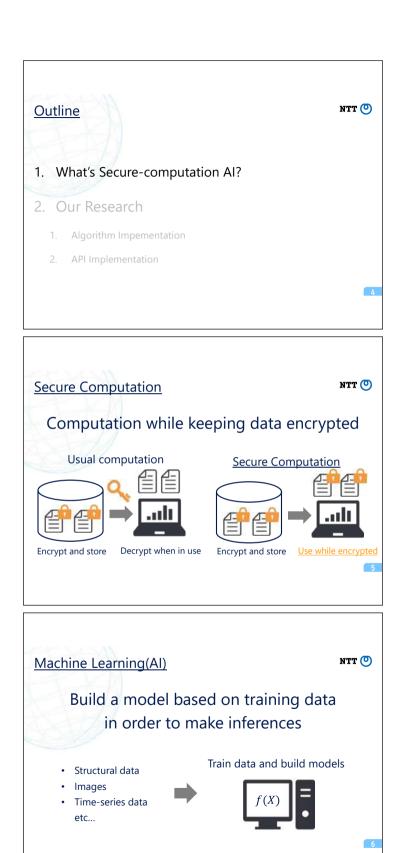
Research on secure computation for machine learning, especially deep learning has been very active in the past few years, and faster methods have been proposed one after another[1]. In addition, there has been research in the area of proposing and implementing easy-to-understand software framework for machine learning researchers and engineers[2]. Thus, various researches on secure computation for machine learning are being conducted, not only on performance but also usability and so on.

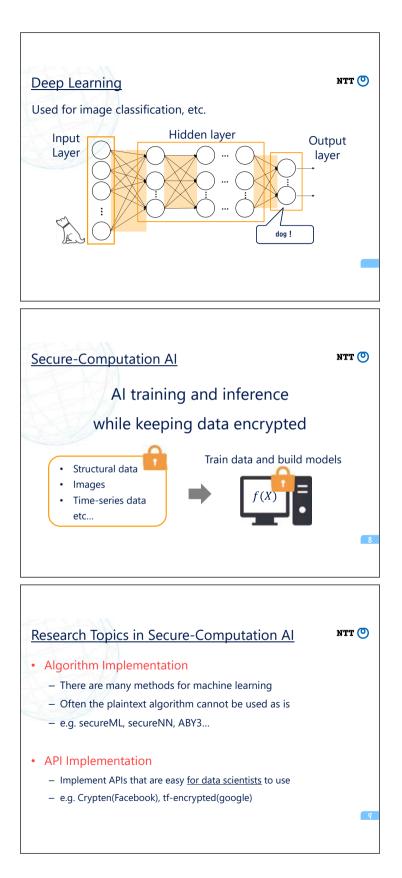
In our research, we have implemented various machine learning methods such as logistic regression and deep learning in secure computation with high speed and high accuracy[3, 4]. Furthermore, we have implemented an software framework for machine learning in secure computation as a Python library[5], with an application programming interface similar to general machine learning libraries. Our secure-computation AI is characterized by high performance in terms of accuracy and processing speed, a rich lineup of analyses, and ease of use, all of which are necessary for an AI library. In this paper, we introduce the performance, the lineup of analysis methods, and application programming an interface of our secure-computation AI library.

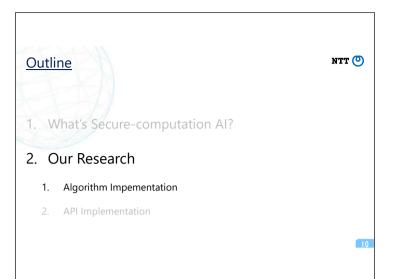
References

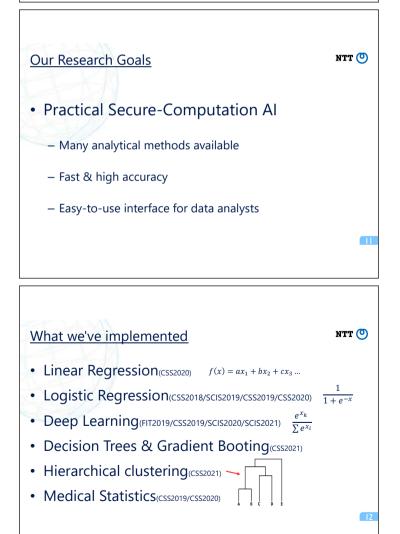
- Wagh, Sameer and Tople, Shruti and Benhamouda, Fabrice and Kushilevitz, Eyal and Mittal, Prateek and Rabin, Tal. Falcon: Honest-majority maliciously secure framework for private deep learning. arXiv preprint arXiv:2004.02229, 2020.
- [2] Knott, Brian and Venkataraman, Shobha and Hannun, Awni and Sengupta, Shubho and Ibrahim, Mark and van der Maaten, Laurens. CrypTen: Secure multi-party computation meets machine learning. arXiv preprint arXiv:2109.00984, 2021.
- [3] Ibuki Mishina, Koki Hamada, Dai Ikarashi and Ryo Kikuchi. Fast and Accurate Logistic Regression and Data Standardization Using Secure Real Number Operations. In CSS(in Japanese), 2020.
- [4] Ibuki Mishina, Koki Hamada and Dai Ikarashi. Realization of Practical Secure Deep Learning. In CSS(in Japanese), 2019.
- [5] Ibuki Mishina, Koki Hamada, Dai Ikarashi and Ryo Kikuchi. A Design and an Implementation of a Python Library for Secure Deep Learning. In SCIS(in Japanese), 2021.

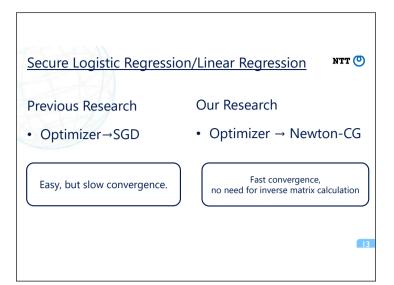










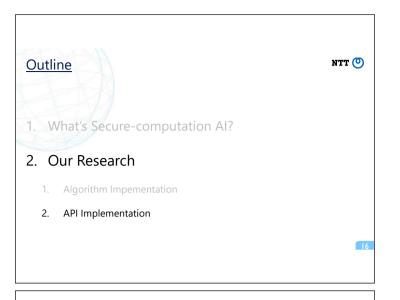




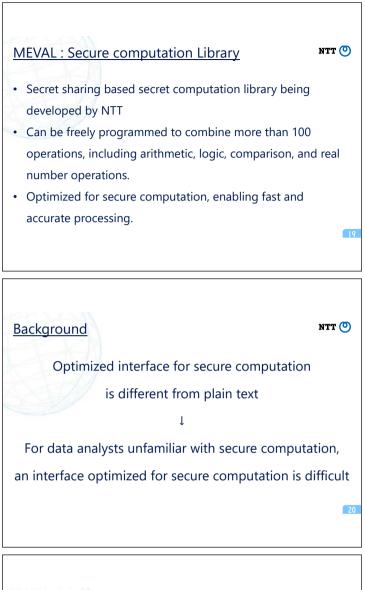
Model : $784 \rightarrow 128 \rightarrow 128 \rightarrow 10(2 \text{ hidden layers})$

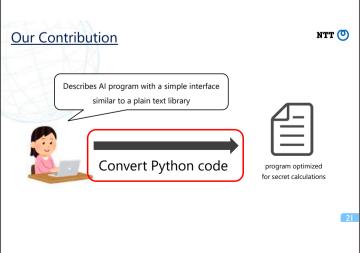
	time[sec]	accuracy[%]
ABY3[MR18]	2700	94
NTT(SCIS2021)*	95	96

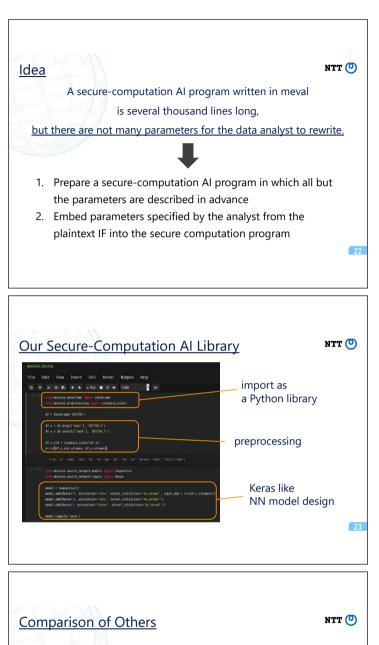
*CPU: 3.50GHz(8core)×2 / RAM: 768GB / NW: 10G











- Crypten(Facebook), tf-encrypted(google)
 - Model : Deep Learning only
 - Processing performance of secure computation is not high
 - Interfaces compatible with Pytorch or tensorflow
- NTT
 - Model : Deep Learning, Decision Trees, Clustering, etc...
 - Fast & high accuracy



• Research Topics in Secure-Computation AI:

- Algorithm Implementation
 - Deep Learning, Logistic Regression, Decision Trees, etc...

- API Impementation
 - Python Library for Secure-Computation AI

November 8–10, 2021, Kyushu University

Possibility of Secret Sharing using EtherCAT

Kosuke Kaneko

Robert T.Huang Entrepreneurship Center of Kyushu University kaneko.kosuke.437@m.kyushu-u.ac.jp

In this presentation, we explain the possibility of Secret Sharing using Ether-CAT(Ethernet for Control Automation Technology) which is an industrial network technology. We implemented an algorithm of Secret Sharing using EtherCAT and evaluated their time performance of encryption/decription. We discuss the possibility of Secret Sharing using EtherCAT based on results of the evaluation.

Possibility of Secret Sharing using EtherCAT

Kosuke Kaneko

Robert T.Huang Entrepreneurship Center of Kyushu University

This research was supported by Skydisc, Inc.

About me

- 2014:
 - Ph.D of Information Science at Kyushu University
- 2014 2016:
 - Assistant Professor at Innovation Center for Educational Resource, Kyushu
 University Library
- 2016 2021:
 - Associate Professor at Cybersecurity Center in Information Infrastracture Iniciative, Kyushu University
- 2021 :
 - Associate Professor at Robert T.Huang Entrepreneurship Center, Kyushu University

Exploring Mathematical and Practical Principles of Secure Computation and Secret Sharing @ IMI, Kyushu University. Nov. 9, 2021.

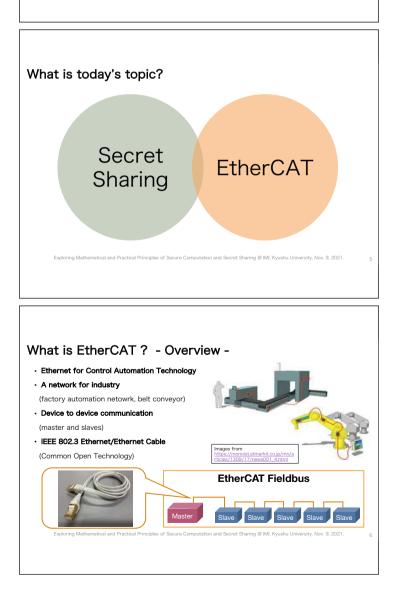
Outline

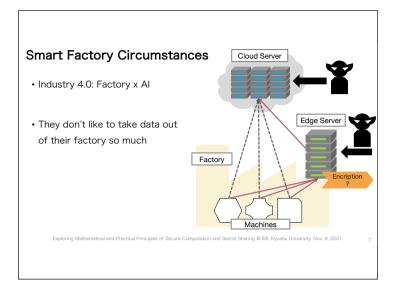
- 1. Research Background and Purpose
 - Smart Factory, EtherCAT
 - Our IDEA of Secret Sharing X EtherCAT
- 2. Method and Implementation
 - Our proposed protocol
- 3. Experiment and ResultCalculation time for encryption/decription
- 4. Conclusion and Discussion

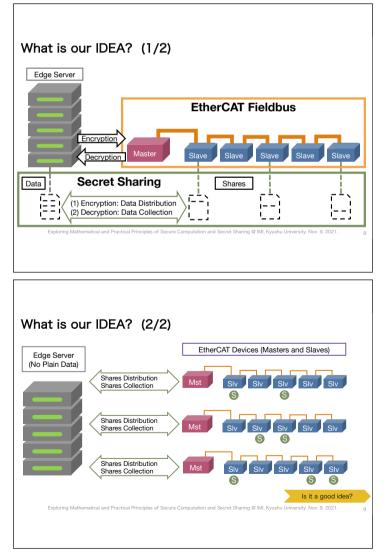
tical and Practical Principles of Secure Computation and Secret Sharing @ IMI, Kyushu University. Nov. 9, 2021

Reserch Background

e Computation and Secret Sharing @ IML Kyushu University, Nov. 9, 2021







Research Purpose

- Investigation for discussing possibility of Secret Sharing with EtherCAT
- Evaluation: Calculation time for encryption/decryption

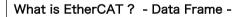
utation and Secret Sharing @ IML Kyushu University, Nov. 9, 2021

- To investigate calculation time by changing situations
 - Number of slaves in EtherCAT fieldbus
 - Number of shares for Secret Sharing

Exploring Mathematical and Practical Principles of Secure Com-

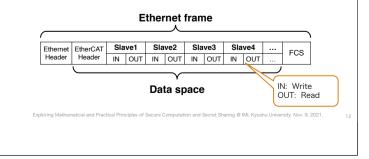
Number of required shares for Secret Sharing

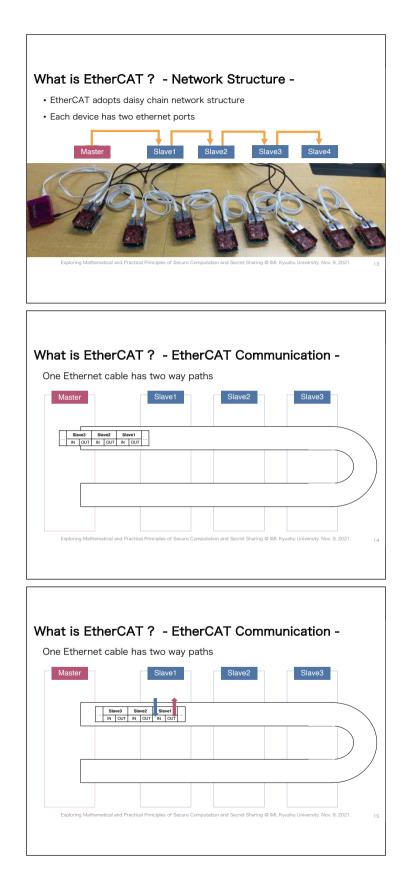
Method and Implementation

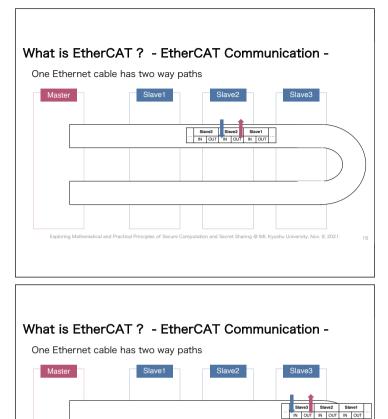


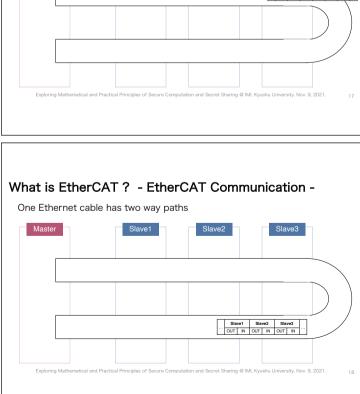
EtherCAT is based on Ethernet:

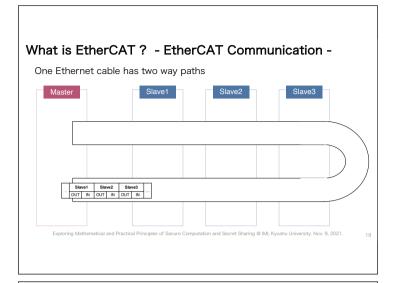
Data frame for communication is Ethernet frame.

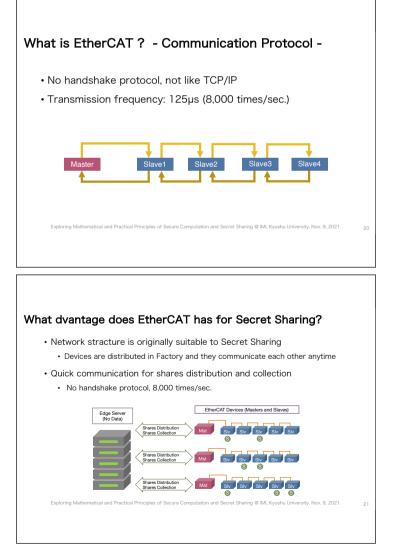


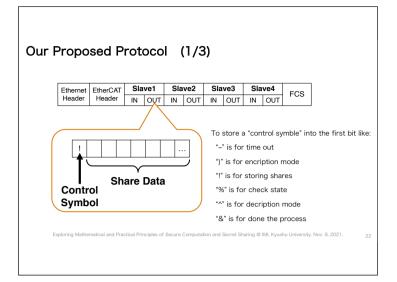


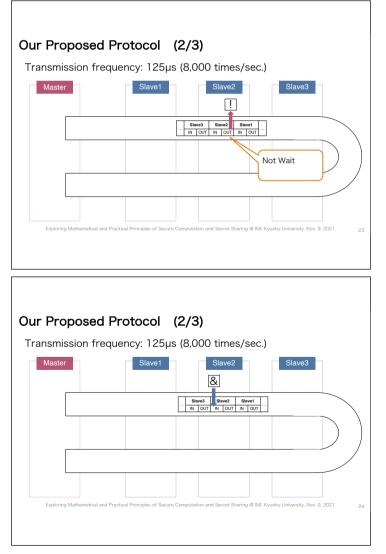


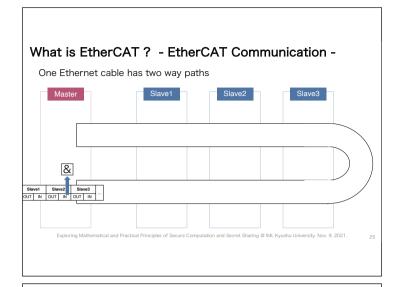






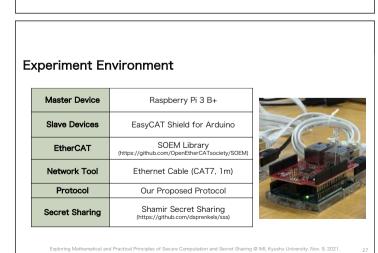


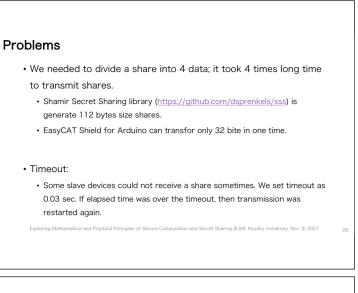


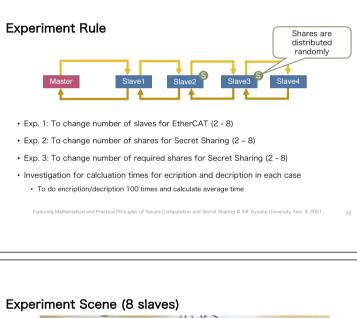


Experiment and Result

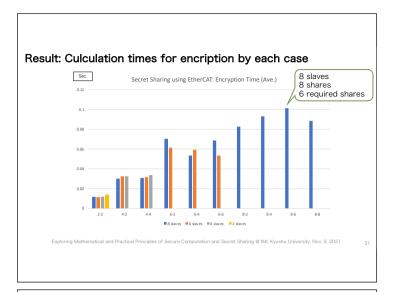
ation and Secret Sharing @ IMI, Kyushu University. Nov. 9, 2021

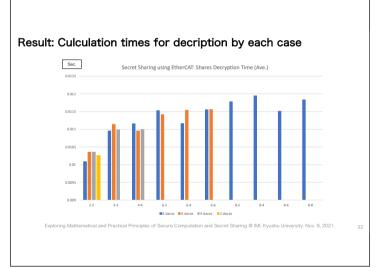


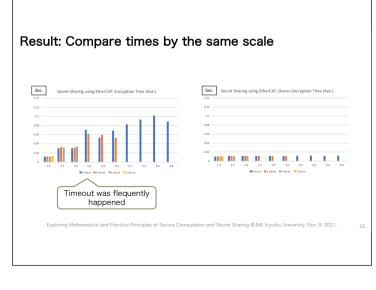


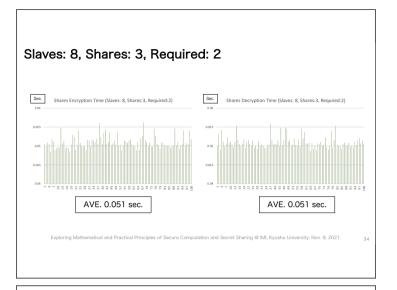


atical and Practical Principles of Secure Computation and Secret Sharing @ MK, Kyushu University, N









Conclusion and Discussion

Conclusion

- Calculation times for encryption/decryption were significantly influenced by number of shares, but it were not so much influenced by number of slaves and number of required shares.
- If it was good condition (no timeout), it took about 0.05 sec. for encryption/decryption.

Discussion Time

Exploring Mathematical and Practical Principles of Secure Computation and Secret Sharing @ IMI, Kyushu University. Nov. 9, 2021.

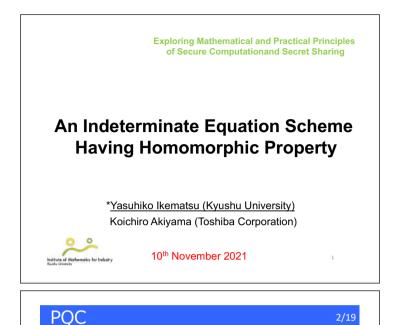
November 8–10, 2021, Kyushu University

An indeterminate equation scheme having homomorphic property

Yasuhiko Ikematsu

Institute of Mathematics for Industry, Kyushu University ikematsu@imi.kyushu-u.ac.jp

Indeterminate encryption schemes are public key cryptosystems using indeterminate equations having a solution with small coefficients over a finite field. At Sac 2017, Akiyama et al. proposed an indeterminate encryption scheme "Giophantus(TM)" whose public key is a polynomial in two variables over a finite ring. In this talk, we introduce the construction of the Giophantus scheme and explain that it becomes a somewhat homomorphic encryption (SHE).

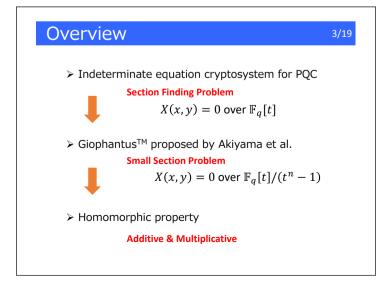


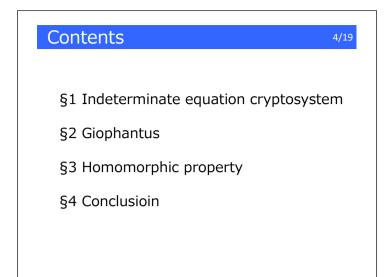
Post-Quantum Cryptography

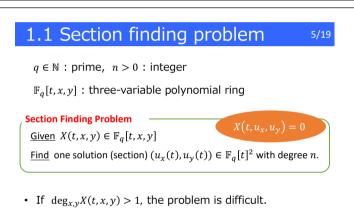
- Lattice base · · · SVP, CVP
- Code base · · · Syndrome decoding problem
- Isogeny base · · · Isogeny path finding problem
- Multivariate base · · · MQ problem

NIST PQC standardization third round in 2020

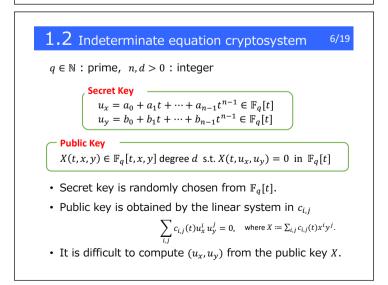
NIST 3rd	Signature	Encryption/KEM
Lattice	2	5
Code	0	3
Isogeny	0	1
Multivariate	2	0
Else	2	0



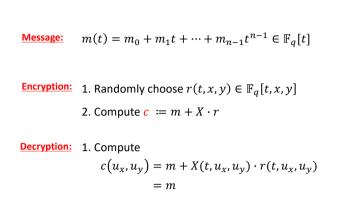


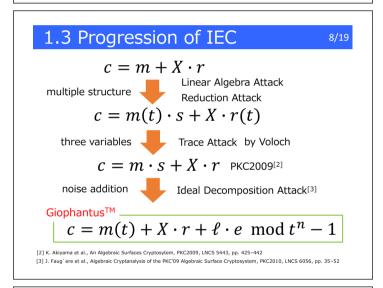


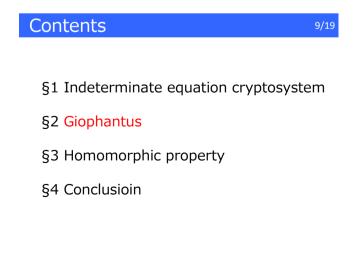
• From this problem, some cryptosystems are constructed.



1.2 Indeterminate equation cryptosystem 7







2.1 Small section problem

 $q \in \mathbb{N}$: prime, n > 0 : integer, l > 0 : small integer

 $X(x,y) \in \mathbb{F}_{q}[t,x,y]/(t^{n}-1)$

- Definition -------

 $(u_x, u_y) \in \mathbb{F}_q[t]^2$ is called a *small section* of *X* if $X(u_x, u_y) = 0$ and $0 \leq \text{their coefficients} \leq l - 1$.

Small Section Problem <u>Given</u> $X(x,y) \in \mathbb{F}_q[t,x,y]/(t^n - 1)$ with a small section, <u>Find</u> one small section (u_x, u_y) of *X*.

Giophantus^[4] is constructed based on this problem.

[4] K. Akiyama et al, A Public-key Encryption Scheme Based on Non-linear Indeterminate Equations (Giophantus), IACR ePrint2017/1241

2.2 Construction

 $q \in \mathbb{N}:$ large prime, $\ n, d > 0:$ integer, $\ l > 0:$ small integer

 $R_{q,n} \coloneqq \mathbb{F}_q[t]/(t^n - 1)$

– Secret Key

 $\begin{array}{l} u_x = a_0 + a_1 t + \cdots + a_{n-1} t^{n-1} \\ u_y = b_0 + b_1 t + \cdots + b_{n-1} t^{n-1} \end{array} \ \, , \mbox{where } 0 \leq a_i, b_i \leq l-1. \end{array}$

- Public Key

- $X(x,y) \in R_{q,n}[x,y]$ degree d s.t. $X(u_x, u_y) = 0$ in $R_{q,n}$
- Secret key is randomly chosen from $\mathbb{F}_q[t]$.
- Public key is obtained by the linear system in $c_{i,j}$
- It is difficult to compute (u_x, u_y) from the public key *X*.

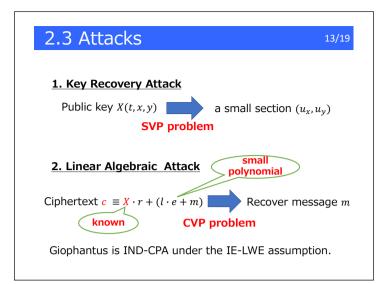
2.2 Construction

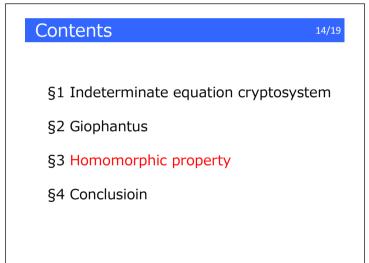
12/19

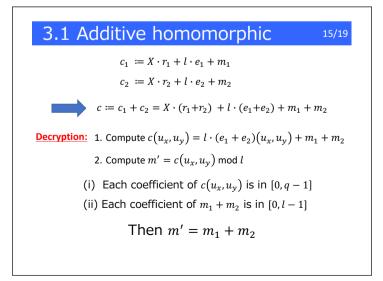
10/19

11/19

Message:	$m(t) = m_0 + m_1 t + \dots + m_{n-1} t^{n-1}, \ 0 \le m_i \le l-1$	
Encryption:	1. Randomly choose $r(x, y) \in \mathbb{F}_q[t, x, y]$	
	2. Randomly choose small $e(x, y) \in \mathbb{F}_q[t, x, y]$	
	3. Compute $c := X \cdot r + l \cdot e + m \mod (q, t^n - 1)$	
Decryption:	1. Compute $c(u_x, u_y) = l \cdot e(u_x, u_y) + m$	
	2. Compute $m' = c(u_x, u_y) \mod l$	
If each coefficient of $c(u_x, u_y)$ is in $[0, q-1]$, then $m = m'$.		
Thus, we	need to take q as follows:	
	$q > l - 1 + l \sum_{k=0}^{\deg_{x,y} e} (k+1)n^k(l-1)^{k+1}$	







3.1 Additive homomorphic

 λ : max of coef of messages m_1, m_2

If the following holds, then $m' = m_1 + m_2$

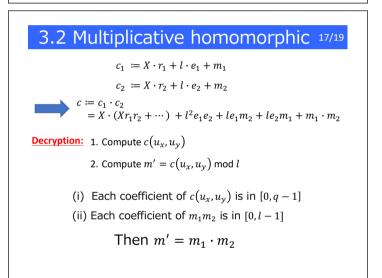
- (i) $l > 2\lambda$
- (ii) $q > 2 \cdot \left(l 1 + l \sum_{k=0}^{\deg e} (k+1) n^k (l-1)^{k+1} \right)$

16/19

• <u>N_a-times additive homomorphic case</u> $c \coloneqq c_1 + c_2 + \dots + c_{N_a}$

If the following holds, then decryption succeeds

• $l > N_a \lambda$ • $q > N_a \left(l - 1 + l \sum_{k=0}^{\deg_{x,y} e} (k+1) n^k (l-1)^{k+1} \right)$



Conclusion 28/19 We introduced an indeterminate equation scheme called "Giophantus". Giophantus is considered to be a scheme for post-quantum cryptography. We explained some homomorphic property of Giophantus. Future work Parameter selection Bootstrapping More efficient HE scheme based on IES



November 8–10, 2021, Kyushu University

Homomorphic Secret Sharing for Multipartite and General Adversary Structures Supporting Parallel Evaluation of Low-Degree Polynomials

Reo Eriguchi (Joint work with Koji Nuida)

The University of Tokyo reo-eriguchi@g.ecc.u-tokyo.ac.jp

Homomorphic secret sharing (HSS) for a function f allows input parties to distribute shares for their private inputs and then locally compute output shares from which the value of f is recovered. HSS can be directly used to obtain a two-round multiparty computation protocol for possibly non-threshold adversary structures whose communication complexity is linear in its share size and independent of the size of f.

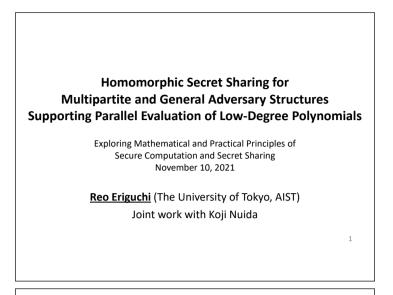
Although several constructions of HSS schemes have been proposed, they do not give a satisfactory solution to practical non-threshold adversary structures Δ . When many parties are involved, Δ is likely to be specified by a general adversary structure rather than by a single threshold. The scheme [2] needs to set a corruption threshold to the maximum size of $X \in \Delta$ and then are inapplicable if Δ contains at least one set of size exceeding their tolerable thresholds. The construction [3] is applicable to any adversary structure but results in exponentially large share size for a specific class of non-threshold adversary structures, e.g., multipartite ones. It is therefore important to construct HSS schemes tailored to given non-threshold adversary structures in order to tolerate corruptions in real-world situations.

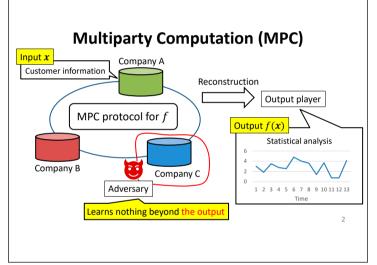
In this talk, we introduce our constructions of HSS schemes tolerating multipartite and general adversary structures and supporting parallel evaluation of a single low-degree polynomial [1]. Our multipartite scheme tolerates a wider class of adversary structures than the previous multipartite one in the particular case of a single evaluation and has exponentially smaller share size than the general construction. While restricting the range of tolerable adversary structures (but still applicable to non-threshold ones), our schemes perform ℓ parallel evaluations with communication complexity approximately $\ell/\log \ell$ times smaller than simply using ℓ independent instances. We also formalize two classes of adversary structures taking into account real-world situations to which the previous threshold schemes are inapplicable. Our schemes then perform O(m) parallel evaluations with almost the same communication cost as a single evaluation, where m is the number of parties.

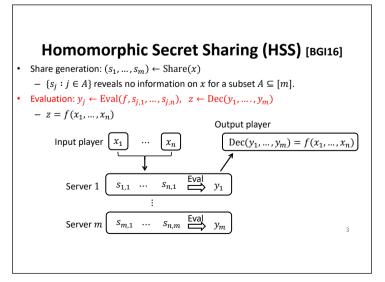
References

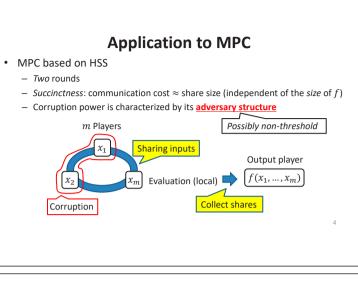
- [2] Y. Ishai, R.W.F. Lai, and G. Malavolta. A geometric approach to homomorphic secret sharing. PKC 2021, pp. 92–119.
- [3] K. Phalakarn, V. Suppakitpaisarn, N. Attrapadung, and K. Matsuura. Constructive t-secure homomorphic secret sharing for low degree polynomials. INDOCRYPT 2020, pp. 763–785.

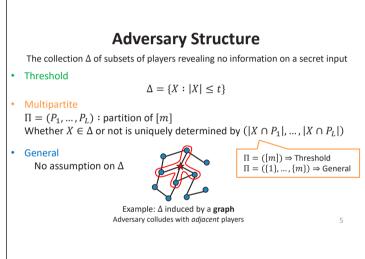
^[1] R. Eriguchi and K. Nuida. Homomorphic secret sharing for multipartite and general adversary structures supporting parallel evaluation of low-degree polynomials. ASIACRYPT 2021, accepted.

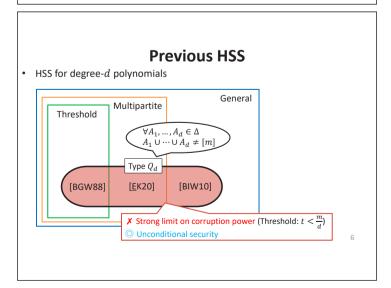


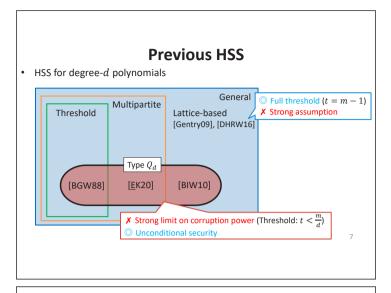


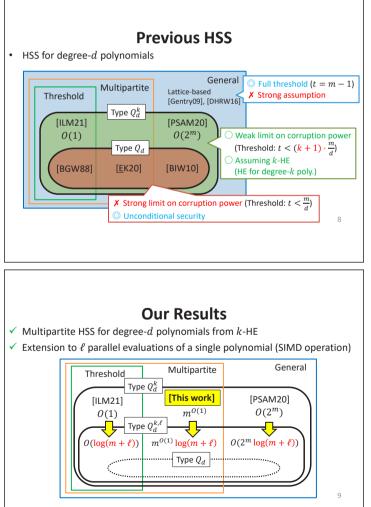


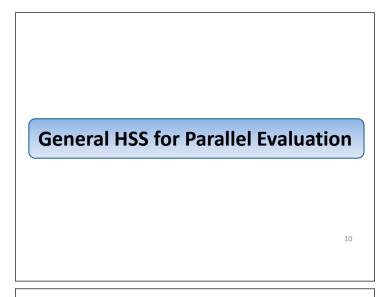


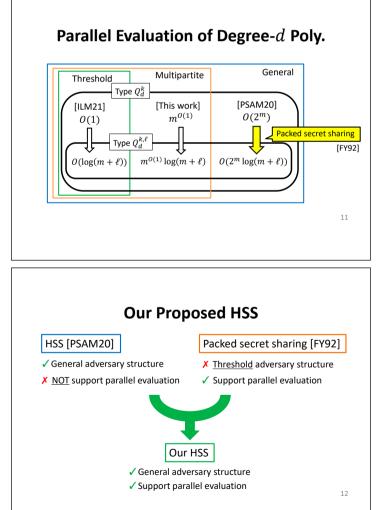


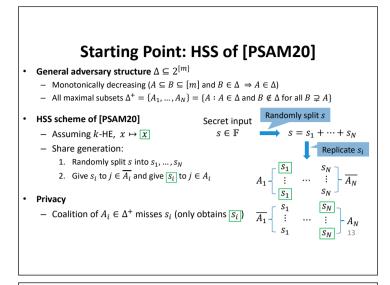


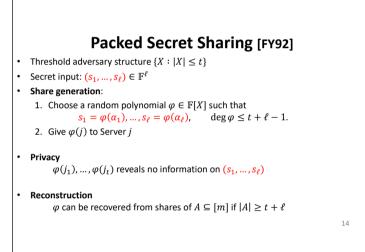


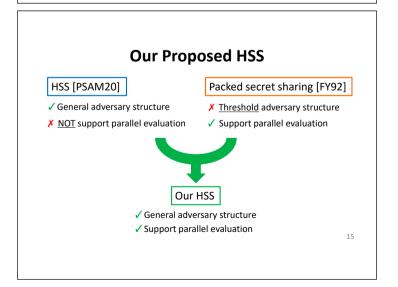


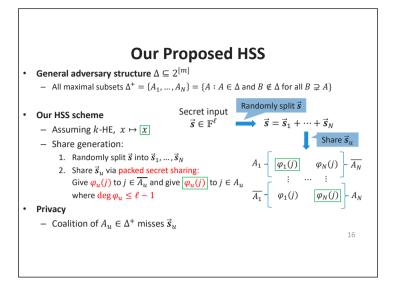












Parallel Evaluation

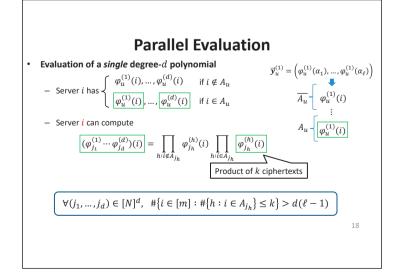
- Evaluation of a *single* degree-*d* polynomial
 - Secret input: $\vec{x}^{(1)}, ..., \vec{x}^{(d)} \in \mathbb{F}^{\ell}$
 - $\vec{x}^{(i)}$ is randomly split into $\vec{x}^{(i)} = \vec{y}_1^{(i)} + \dots + \vec{y}_N^{(i)}$

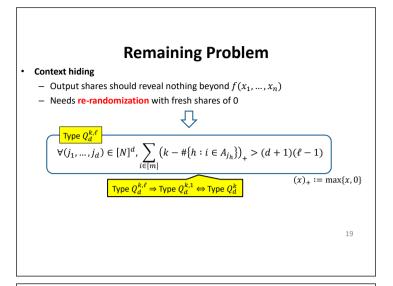
$$- \vec{y}_u^{(i)} = \left(\varphi_u^{(i)}(\alpha_1), \dots, \varphi_u^{(i)}(\alpha_\ell)\right), \deg \varphi_u^{(i)} \le \ell - 1$$

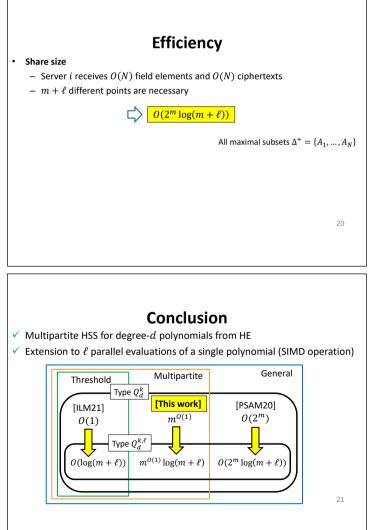
$$\implies \vec{\mathbf{x}}^{(1)} \ast \cdots \ast \vec{\mathbf{x}}^{(d)} = \sum_{j=(j_1,\dots,j_d) \in [N]^d} \vec{\mathbf{y}}_{j_1}^{(1)} \ast \cdots \ast \vec{\mathbf{y}}_{j_d}^{(d)}$$

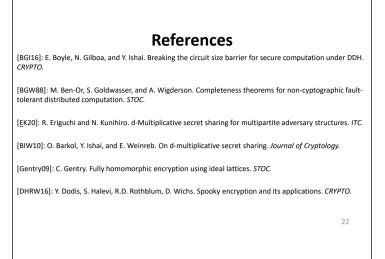
More than $d(\ell-1)$ points of $\varphi_{j_1}^{(1)}\cdots\varphi_{j_d}^{(d)}$ must be collected from servers

* denotes the element-wise product 17









References	
[ILM21]: Y. Ishai, R.W.F. Lai, and G. Malavolta. A geometric approach to homomorphic secret sharing.	РКС.
[PSAM20]: K. Phalakarn, V. Suppakitpaisarn, N. Attrapadung, and K. Matuura. Constructive t-secure homomorphic secret sharing for low degree polynomials. <i>INDOCRYPT</i> .	
[FY92]: M. Franklin and M. Yung. Communication complexity of secure computation. STOC.	
	23
Thank you!	
	24

November 8–10, 2021, Kyushu University

A Comparison of How to Garble Arithmetic and Boolean Circuits - Case of Functional Encryption -

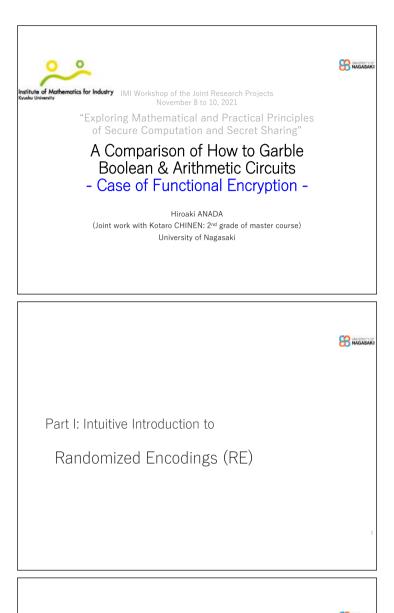
Hiroaki Anada (Joint work with Kotaro Chinen)

University of Nagasaki anada@sun.ac.jp

The technique of garbling circuits that was initiated by Yao [1] is currently one of the fundamental cryptographic primitives. It is generalized and enhanced as the randomized encoding of functions [2, 3], which can treat not only boolean circuits but also arithmetic circuits. In this talk, after warming up with examples of randomized encoding, we focus into garbling encryption circuits of functional encryption following the work of Goyal, Koppla and Waters [4]. We see that there is a gap between "boolean" and "arithmetic" in security proofs; in the case of boolean, we only have to select one of two evaluated keys, but in the case of arithmetic, we must evaluate a key-value for any given input.

References

- Andrew Chi-Chih Yao. How to generate and exchange secrets (extended abstract). In 27th Annual Symposium on Foundations of Computer Science, Toronto, Canada, 27-29 October 1986, pages 162–167. IEEE Computer Society, 1986.
- [2] Benny Applebaum, Yuval Ishai, and Eyal Kushilevitz. How to garble arithmetic circuits. In Rafail Ostrovsky, editor, *IEEE 52nd Annual Symposium on Foundations of Computer Science, FOCS* 2011, Palm Springs, CA, USA, October 22-25, 2011, pages 120–129. IEEE Computer Society, 2011.
- [3] Benny Applebaum. Garbled circuits as randomized encodings of functions: a primer. In Yehuda Lindell, editor, *Tutorials on the Foundations of Cryptography*, pages 1–44. Springer International Publishing, 2017.
- [4] Rishab Goyal, Venkata Koppula, and Brent Waters. Semi-adaptive security and bundling functionalities made generic and easy. In Martin Hirt and Adam D. Smith, editors, *Theory of Cryptography* - 14th International Conference, TCC 2016-B, Beijing, China, October 31 - November 3, 2016, Proceedings, Part II, volume 9986 of Lecture Notes in Computer Science, pages 361–388, 2016.

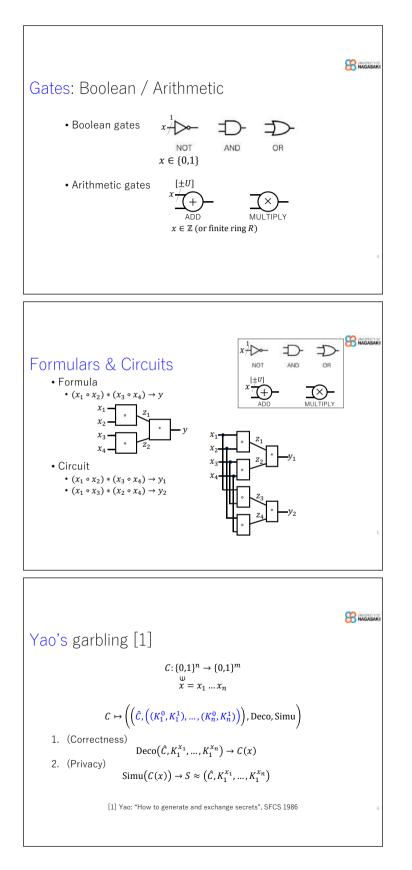


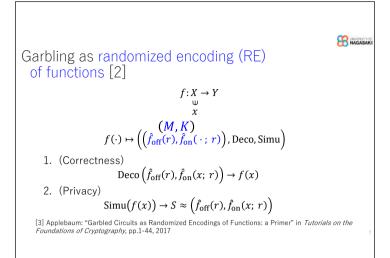
Garbling techniques

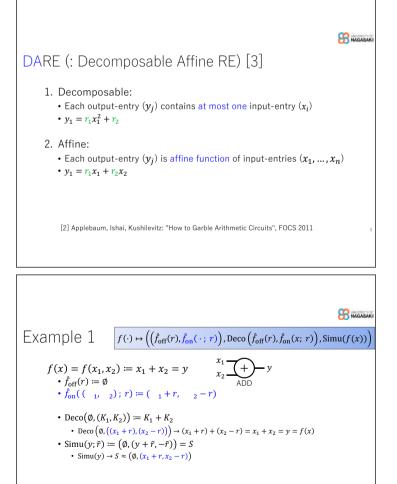
 Yao: "How to generate and exchange secrets", SFCS 1986
 Applebaum, Ishai, Kushilevitz: "How to Garble Arithmetic Circuits", FOCS 2011

→ GC-based secure computation ©

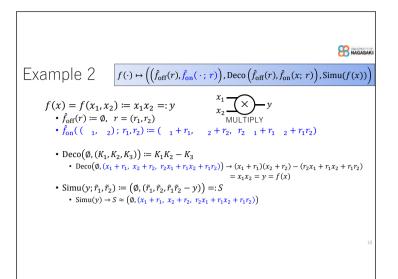
 \rightarrow This talk: Garbling functional encryption circuit (\circledast ?)

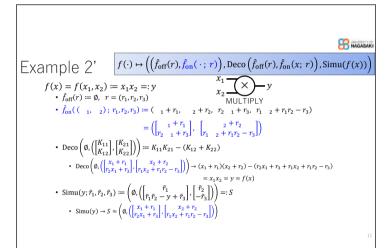


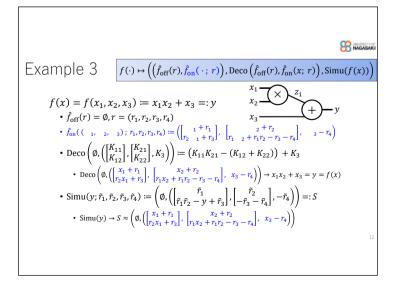


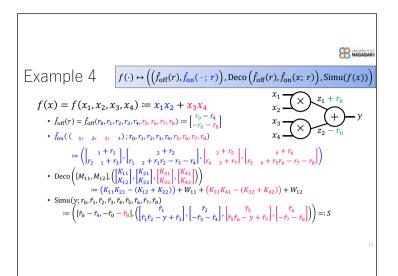


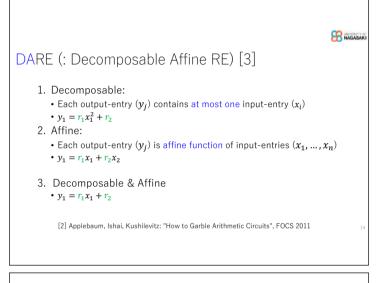
[2] Applebaum, Ishai, Kushilevitz: "How to Garble Arithmetic Circuits", FOCS 2011, pp.120-129
 [3] Applebaum: "Garbled Circuits as Randomized Encodings of Functions: a Primer" in *Tutorials on the Foundations of Cryptography*, pp.1-44, 2017

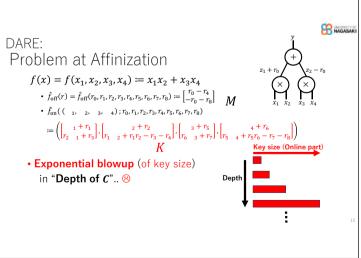


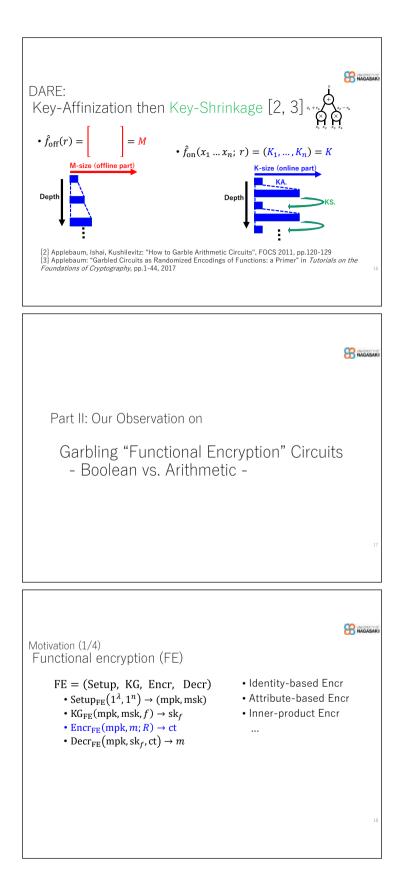


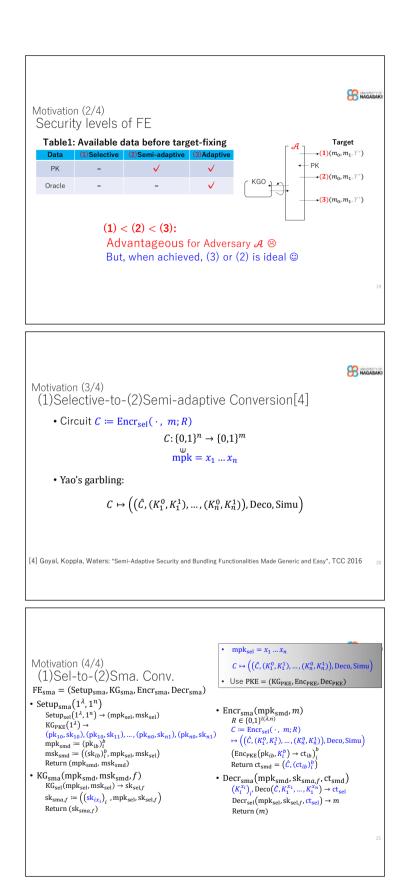


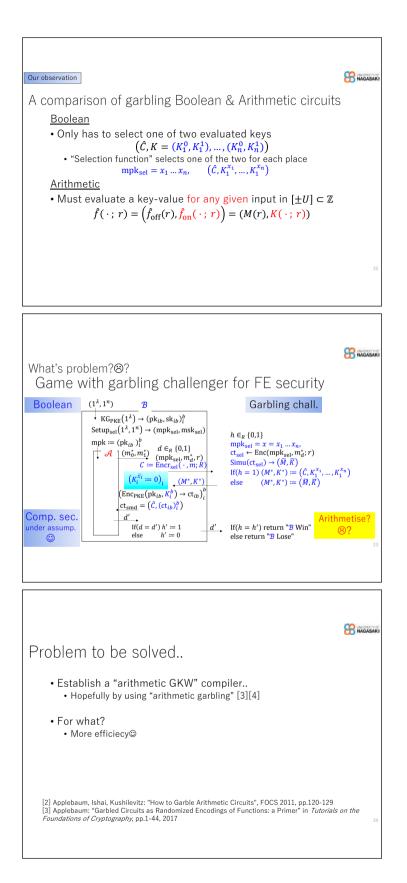


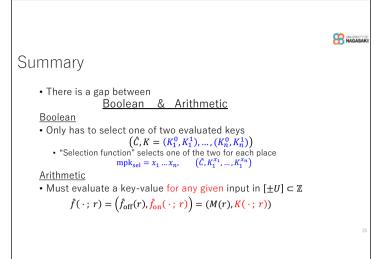












Emme Thank you for your attention! MI レクチャーノートシリーズ刊行にあたり

本レクチャーノートシリーズは、文部科学省 21 世紀 COE プログラム「機 能数理学の構築と展開」(H.15-19 年度)において作成した COE Lecture Notes の続刊であり、文部科学省大学院教育改革支援プログラム「産業界が求める 数学博士と新修士養成」(H19-21 年度)および、同グローバル COE プログラ ム「マス・フォア・インダストリ教育研究拠点」(H.20-24 年度)において行 われた講義の講義録として出版されてきた。平成 23 年 4 月のマス・フォア・ インダストリ研究所(IMI)設立と平成 25 年 4 月の IMI の文部科学省共同利用・ 共同研究拠点として「産業数学の先進的・基礎的共同研究拠点」の認定を受け、 今後、レクチャーノートは、マス・フォア・インダストリに関わる国内外の 研究者による講義の講義録、会議録等として出版し、マス・フォア・インダ ストリの本格的な展開に資するものとする。

> 平成 30 年 10 月 マス・フォア・インダストリ研究所 所長 佐伯修

2021年度 九州大学マス・フォア・インダストリ研究所 共同利用研究集会

秘密計算・秘密分散の数理と実用の探求

- 発 行 九州大学マス・フォア・インダストリ研究所
- 九州大学大学院数理学府 〒819-0395 福岡市西区元岡744 九州大学数理・IMI 事務室 TEL 092-802-4402 FAX 092-802-4405 URL https://www.imi.kyushu-u.ac.jp/
- 印 刷 城島印刷株式会社 〒810-0012 福岡市中央区白金 2 丁目 9 番 6 号 TEL 092-531-7102 FAX 092-524-4411

発 行 2022年2月9日

編 集 穴田啓晃,池松泰彦,縫田光司,大畑幸矢,Yuntao Wang

Issue	Author / Editor	Title	Published
COE Lecture Note	Mitsuhiro T. NAKAO Kazuhiro YOKOYAMA	Computer Assisted Proofs - Numeric and Symbolic Approaches - 199pages	August 22, 2006
COE Lecture Note	M.J.Shai HARAN	Arithmetical Investigations - Representation theory, Orthogonal polynomials and Quantum interpolations- 174pages	August 22, 2006
COE Lecture Note Vol.3	Michal BENES Masato KIMURA Tatsuyuki NAKAKI	Proceedings of Czech-Japanese Seminar in Applied Mathematics 2005 155pages	October 13, 2006
COE Lecture Note Vol.4	宮田 健治	辺要素有限要素法による磁界解析 - 機能数理学特別講義 21pages	May 15, 2007
COE Lecture Note Vol.5	Francois APERY	Univariate Elimination Subresultants - Bezout formula, Laurent series and vanishing conditions - 89pages	September 25, 2007
COE Lecture Note Vol.6	Michal BENES Masato KIMURA Tatsuyuki NAKAKI	Proceedings of Czech-Japanese Seminar in Applied Mathematics 2006 209pages	October 12, 2007
COE Lecture Note Vol.7	若山 正人 中尾 充宏	九州大学産業技術数理研究センター キックオフミーティング 138pages	October 15, 2007
COE Lecture Note Vol.8	Alberto PARMEGGIANI	Introduction to the Spectral Theory of Non-Commutative Harmonic Oscillators 233pages	January 31, 2008
COE Lecture Note Vol.9	Michael I.TRIBELSKY	Introduction to Mathematical modeling 23pages	February 15, 2008
COE Lecture Note Vol.10	Jacques FARAUT	Infinite Dimensional Spherical Analysis 74pages	March 14, 2008
COE Lecture Note Vol.11	Gerrit van DIJK	Gelfand Pairs And Beyond 60pages	August 25, 2008
COE Lecture Note Vol.12	Faculty of Mathematics, Kyushu University	Consortium "MATH for INDUSTRY" First Forum 87pages	September 16, 2008
COE Lecture Note Vol.13	九州大学大学院 数理学研究院	プロシーディング「損保数理に現れる確率モデル」 — 日新火災・九州大学 共同研究2008年11月 研究会 — 82pages	February 6, 2009

Issue	Author / Editor	Title	Published
COE Lecture Note Vol.14	Michal Beneš, Tohru Tsujikawa Shigetoshi Yazaki	Proceedings of Czech-Japanese Seminar in Applied Mathematics 2008 77pages	February 12, 2009
COE Lecture Note Vol.15	Faculty of Mathematics, Kyushu University	International Workshop on Verified Computations and Related Topics 129pages	February 23, 2009
COE Lecture Note Vol.16	Alexander Samokhin	Volume Integral Equation Method in Problems of Mathematical Physics 50pages	February 24, 2009
COE Lecture Note Vol.17	午嶋 徹 及川 正行 梶原 健司 辻 英一 福本 康秀	非線形波動の数理と物理 66pages	February 27, 2009
COE Lecture Note Vol.18	Tim Hoffmann	Discrete Differential Geometry of Curves and Surfaces 75pages	April 21, 2009
COE Lecture Note Vol.19	Ichiro Suzuki	The Pattern Formation Problem for Autonomous Mobile Robots —Special Lecture in Functional Mathematics— 23pages	April 30, 2009
COE Lecture Note Vol.20	Yasuhide Fukumoto Yasunori Maekawa	Math-for-Industry Tutorial: Spectral theories of non-Hermitian operators and their application 184pages	June 19, 2009
COE Lecture Note Vol.21	Faculty of Mathematics, Kyushu University	Forum "Math-for-Industry" Casimir Force, Casimir Operators and the Riemann Hypothesis 95pages	November 9, 2009
COE Lecture Note Vol.22	Masakazu Suzuki Hoon Hong Hirokazu Anai Chee Yap Yousuke Sato Hiroshi Yoshida	The Joint Conference of ASCM 2009 and MACIS 2009: Asian Symposium on Computer Mathematics Mathematical Aspects of Computer and Information Sciences 436pages	December 14, 2009
COE Lecture Note Vol.23	荒川 恒男 金子 昌信	多重ゼータ値入門 111pages	February 15, 2010
COE Lecture Note Vol.24	Fulton B.Gonzalez	Notes on Integral Geometry and Harmonic Analysis 125pages	March 12, 2010
COE Lecture Note Vol.25	Wayne Rossman	Discrete Constant Mean Curvature Surfaces via Conserved Quantities 130pages	May 31, 2010
COE Lecture Note Vol.26	Mihai Ciucu	Perfect Matchings and Applications 66pages	July 2, 2010

Issue	Author / Editor	Title	Published
COE Lecture Note Vol.27	九州大学大学院 数理学研究院	Forum "Math-for-Industry" and Study Group Workshop Information security, visualization, and inverse problems, on the basis of optimization techniques 100pages	October 21, 2010
COE Lecture Note Vol.28	ANDREAS LANGER	MODULAR FORMS, ELLIPTIC AND MODULAR CURVES LECTURES AT KYUSHU UNIVERSITY 2010 62pages	November 26, 2010
COE Lecture Note Vol.29	木田 雅成 原田 昌晃 横山 俊一	Magma で広がる数学の世界 157pages	December 27, 2010
COE Lecture Note Vol.30	原 隆 松井 卓 廣島 文生	Mathematical Quantum Field Theory and Renormalization Theory 201pages	January 31, 2011
COE Lecture Note Vol.31	若山 正人 福本 康秀 高木 剛 山本 昌宏	Study Group Workshop 2010 Lecture & Report 128pages	February 8, 2011
COE Lecture Note Vol.32	Institute of Mathematics for Industry, Kyushu University	Forum "Math-for-Industry" 2011 "TSUNAMI-Mathematical Modelling" Using Mathematics for Natural Disaster Prediction, Recovery and Provision for the Future 90pages	September 30, 2011
COE Lecture Note Vol.33	若山 正人福本 康秀高木 剛山本 昌宏	Study Group Workshop 2011 Lecture & Report 140pages	October 27, 2011
COE Lecture Note Vol.34	Adrian Muntean Vladimír Chalupecký	Homogenization Method and Multiscale Modeling 72pages	October 28, 2011
COE Lecture Note Vol.35	横山 俊一 夫 紀恵 林 卓也	計算機代数システムの進展 210pages	November 30, 2011
COE Lecture Note Vol.36	Michal Beneš Masato Kimura Shigetoshi Yazaki	Proceedings of Czech-Japanese Seminar in Applied Mathematics 2010 107pages	January 27, 2012
COE Lecture Note Vol.37	 若山 正人 高木 剛 Kirill Morozov 平岡 裕章 木村 正人 白井 朋之 西井 龍一郎 六井 宏和 「六井 康秀 	平成23年度 数学・数理科学と諸科学・産業との連携研究ワーク ショップ 拡がっていく数学 〜期待される"見えない力"〜 154pages	February 20, 2012

Issue	Author / Editor	Title	Published
COE Lecture Note Vol.38	Fumio Hiroshima Itaru Sasaki Herbert Spohn Akito Suzuki	Enhanced Binding in Quantum Field Theory 204pages	March 12, 2012
COE Lecture Note Vol.39	Institute of Mathematics for Industry, Kyushu University	Multiscale Mathematics; Hierarchy of collective phenomena and interrelations between hierarchical structures 180pages	March 13, 2012
COE Lecture Note Vol.40	井ノ口順一 太田 泰広 寛郎 王郎 梶原 健司 松浦 望	離散可積分系・離散微分幾何チュートリアル2012 152pages	March 15, 2012
COE Lecture Note Vol.41	Institute of Mathematics for Industry, Kyushu University	Forum "Math-for-Industry" 2012 "Information Recovery and Discovery" 91pages	October 22, 2012
COE Lecture Note Vol.42	佐伯 修 若山 正人 山本 昌宏	Study Group Workshop 2012 Abstract, Lecture & Report 178pages	November 19, 2012
COE Lecture Note Vol.43	Institute of Mathematics for Industry, Kyushu University	Combinatorics and Numerical Analysis Joint Workshop 103pages	December 27, 2012
COE Lecture Note Vol.44	萩原 学	モダン符号理論からポストモダン符号理論への展望 107pages	January 30, 2013
COE Lecture Note Vol.45	金山 寛	Joint Research Workshop of Institute of Mathematics for Industry (IMI), Kyushu University "Propagation of Ultra-large-scale Computation by the Domain- decomposition-method for Industrial Problems (PUCDIP 2012)" 121pages	February 19, 2013
COE Lecture Note Vol.46	西井 龍映 栄 伸一郎 岡田 勘三 落 啓之 小磯 深幸 斎藤 新悟 白井 朋之	科学・技術の研究課題への数学アプローチ 一数学モデリングの基礎と展開— 325pages	February 28, 2013
COE Lecture Note Vol.47	SOO TECK LEE	BRANCHING RULES AND BRANCHING ALGEBRAS FOR THE COMPLEX CLASSICAL GROUPS 40pages	March 8, 2013
COE Lecture Note Vol.48	溝口 佳寛 脇 隼人 平坂 貢 谷口 哲至 鳥袋 修	博多ワークショップ「組み合わせとその応用」 124pages	March 28, 2013

Issue	Author / Editor	Title	Published
COE Lecture Note Vol.49	照井 章 功任 濱田 龍義 横山 俊一 六井 宏和 横田 博史	マス・フォア・インダストリ研究所 共同利用研究集会 II 数式処理研究と産学連携の新たな発展 137pages	August 9, 2013
MI Lecture Note Vol.50	Ken Anjyo Hiroyuki Ochiai Yoshinori Dobashi Yoshihiro Mizoguchi Shizuo Kaji	Symposium MEIS2013: Mathematical Progress in Expressive Image Synthesis 154pages	October 21, 2013
MI Lecture Note Vol.51	Institute of Mathematics for Industry, Kyushu University	Forum "Math-for-Industry" 2013 "The Impact of Applications on Mathematics" 97pages	October 30, 2013
MI Lecture Note Vol.52	佐伯 修 岡田 勘三 高木 剛 若山 正人 山本 昌宏	Study Group Workshop 2013 Abstract, Lecture & Report 142pages	November 15, 2013
MI Lecture Note Vol.53	四方 義啓 櫻井 幸一 安田 貴徳 Xavier Dahan	平成25年度 九州大学マス・フォア・インダストリ研究所 共同利用研究集会 安全・安心社会基盤構築のための代数構造 〜サイバー社会の信頼性確保のための数理学〜 158pages	December 26, 2013
MI Lecture Note Vol.54	Takashi Takiguchi Hiroshi Fujiwara	Inverse problems for practice, the present and the future 93pages	January 30, 2014
MI Lecture Note Vol.55	 栄 伸一郎 溝口 佳寛 脇 隼人 渋田 敬史 	Study Group Workshop 2013 数学協働プログラム Lecture & Report 98pages	February 10, 2014
MI Lecture Note Vol.56	Yoshihiro Mizoguchi Hayato Waki Takafumi Shibuta Tetsuji Taniguchi Osamu Shimabukuro Makoto Tagami Hirotake Kurihara Shuya Chiba	Hakata Workshop 2014 ~ Discrete Mathematics and its Applications ~ 141pages	March 28, 2014
MI Lecture Note Vol.57	Institute of Mathematics for Industry, Kyushu University	Forum "Math-for-Industry" 2014: "Applications + Practical Conceptualization + Mathematics = fruitful Innovation" 93pages	October 23, 2014
MI Lecture Note Vol.58	安生健一 落合啓之	Symposium MEIS2014: Mathematical Progress in Expressive Image Synthesis 135pages	November 12, 2014

Issue	Author / Editor	Title	Published
MI Lecture Note Vol.59	西井 龍 開田	Study Group Workshop 2014 数学協働プログラム Abstract, Lecture & Report 196pages	November 14, 2014
MI Lecture Note Vol.60	西浦 博	平成26年度九州大学 IMI 共同利用研究・研究集会(I) 感染症数理モデルの実用化と産業及び政策での活用のための新 たな展開 120pages	November 28, 2014
MI Lecture Note Vol.61	溝口 佳寛 Jacques Garrigue 萩原 学 Reynald Affeldt	研究集会 高信頼な理論と実装のための定理証明および定理証明器 Theorem proving and provers for reliable theory and implementations (TPP2014) 138pages	February 26, 2015
MI Lecture Note Vol.62	白井 朋之	Workshop on "β-transformation and related topics" 59pages	March 10, 2015
MI Lecture Note Vol.63	白井 朋之	Workshop on "Probabilistic models with determinantal structure" 107pages	August 20, 2015
MI Lecture Note Vol.64	落合 啓之 土橋 宜典	Symposium MEIS2015: Mathematical Progress in Expressive Image Synthesis 124pages	September 18, 2015
MI Lecture Note Vol.65	Institute of Mathematics for Industry, Kyushu University	Forum "Math-for-Industry" 2015 "The Role and Importance of Mathematics in Innovation" 74pages	October 23, 2015
MI Lecture Note Vol.66	岡田 勘三 藤澤 克己 白井 朋之 若山 正人 脇 隼人 Philip Broadbridge 山本 昌宏	Study Group Workshop 2015 Abstract, Lecture & Report 156pages	November 5, 2015
MI Lecture Note Vol.67	Institute of Mathematics for Industry, Kyushu University	IMI-La Trobe Joint Conference "Mathematics for Materials Science and Processing" 66pages	February 5, 2016
MI Lecture Note Vol.68	古庄 英和 小谷 久寿 新甫 洋史	結び目と Grothendieck-Teichmüller 群 116pages	February 22, 2016
MI Lecture Note Vol.69	土橋 宜典 鍛治 静雄	Symposium MEIS2016: Mathematical Progress in Expressive Image Synthesis 82pages	October 24, 2016
MI Lecture Note Vol.70	Institute of Mathematics for Industry, Kyushu University	Forum "Math-for-Industry" 2016 "Agriculture as a metaphor for creativity in all human endeavors" 98pages	November 2, 2016
MI Lecture Note Vol.71	小磯 深幸 二宮 嘉行 山本 昌宏	Study Group Workshop 2016 Abstract, Lecture & Report 143pages	November 21, 2016

Issue	Author / Editor	Title	Published
MI Lecture Note Vol.72	新井 朝雄 小嶋 泉 廣島 文生	Mathematical quantum field theory and related topics 133pages	January 27, 2017
MI Lecture Note Vol.73	穴田 啓晃 Kirill Morozov 須賀 祐治 奥村 伸也 櫻井 幸一	Secret Sharing for Dependability, Usability and Security of Network Storage and Its Mathematical Modeling 211pages	March 15, 2017
MI Lecture Note Vol.74	QUISPEL, G. Reinout W. BADER, Philipp MCLAREN, David I. TAGAMI, Daisuke	IMI-La Trobe Joint Conference Geometric Numerical Integration and its Applications 71pages	March 31, 2017
MI Lecture Note Vol.75	手塚 集 田上 大助 山本 昌宏	Study Group Workshop 2017 Abstract, Lecture & Report 118pages	October 20, 2017
MI Lecture Note Vol.76	宇田川誠一	Tzitzéica 方程式の有限間隙解に付随した極小曲面の構成理論 一Tzitzéica 方程式の楕円関数解を出発点として一 68pages	August 4, 2017
MI Lecture Note Vol.77	松谷 茂樹 佐伯 修 中川 淳一 田上 大助 上坂 正晃 Pierluigi Cesana 濵田 裕康	平成29年度 九州大学マス・フォア・インダストリ研究所 共同利用研究集会 (I) 結晶の界面, 転位, 構造の数理 148pages	December 20, 2017
MI Lecture Note Vol.78	 瀧澤 重志 小林 和博 佐藤憲 赤 本 一郎 斎藤 死明 間瀬 正啓 藤澤 克樹 神山 直之 	平成29年度 九州大学マス・フォア・インダストリ研究所 プロジェクト研究 研究集会 (I) 防災・避難計画の数理モデルの高度化と社会実装へ向けて 136pages	February 26, 2018
MI Lecture Note Vol.79	神山 直之 畔上 秀幸	平成29年度 AIMaP チュートリアル 最適化理論の基礎と応用 96pages	February 28, 2018
MI Lecture Note Vol.80	Kirill Morozov Hiroaki Anada Yuji Suga	IMI Workshop of the Joint Research Projects Cryptographic Technologies for Securing Network Storage and Their Mathematical Modeling 116pages	March 30, 2018
MI Lecture Note Vol.81	Tsuyoshi Takagi Masato Wakayama Keisuke Tanaka Noboru Kunihiro Kazufumi Kimoto Yasuhiko Ikematsu	IMI Workshop of the Joint Research Projects International Symposium on Mathematics, Quantum Theory, and Cryptography 246pages	September 25, 2019
MI Lecture Note Vol.82	池森 俊文	令和2年度 AIMaP チュートリアル 新型コロナウイルス感染症にかかわる諸問題の数理 145pages	March 22, 2021

Issue	Author / Editor	Title	Published
MI Lecture Note Vol.83	早川健太郎 軸丸 芳揮 横須賀洋平 可香谷 隆 林 和希 堺 雄亮	シェル理論・膜理論への微分幾何学からのアプローチと その建築曲面設計への応用 49pages	July 28, 2021
MI Lecture Note Vol.84	Taketoshi Kawabe Yoshihiro Mizoguchi Junichi Kako Masakazu Mukai Yuji Yasui	SICE-JSAE-AIMaP Tutorial Advanced Automotive Control and Mathematics 110pages	December 27, 2021



九州大学マス・フォア・インダストリ研究所 九州大学大学院 数理学府

〒819-0395 福岡市西区元岡744 TEL 092-802-4402 FAX 092-802-4405 URL http://www.imi.kyushu-u.ac.jp/